

# DESIGN OF ZETA CONVERTOR WITH IMPROVED POWER QUALITY FOR BRUSHLESS DC DRIVES

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**ABSTRACT:** *Development of a quality improved zeta converter feeding brushless DC (BLDC) drives. 1- $\theta$  AC, rectified using diode bridge rectification (DBR) and a discontinuous current interval in an inductor of zeta converter in front of inverter is studied in this paper. The zeta work as a pre regulator when it is operating in discontinuous inductor current interval. In this scheme only one sensor used to control voltage of zeta converter for the large range of speed control of the brushless DC drive. This topology enables the switching of voltage source inverter on fundamental frequency to minimize the switching losses. The suggested scheme for the Brushless DC drive is developed and its operation and results are observed in MATLAB for attaining the improved power factor for the large range speed control. The achieved results are in the allowable limits of worldwide power criteria.*

## I. INTRODUCTION

Brush less DC drive has gained much attention in past decade due to wide range of speed, less Electromagnetic interference (EMI), high ruggedness, high flux density, comparatively high efficiency, and minimize the maintenance requirements [1]. Aforementioned properties grapes the attention from wide areas like aerospace, industrial tools, hybrid automation, in robots like actuators and position sensors, home and industry ventilation, power plants and other household applications. 3-phase BLDC motor generally encompasses of 3-phase stator winding and PM (Permanent Magnet) rotor which makes it synchronous. As name suggest that it consist on PM rotor and brush less commutator which rejects the sparking, overheating, brush losses, low Electromagnetic Interference (EMI) and maintenance cost. It having same torque speed characteristics as of typically used DC motors. The commutation assembly works electronically and so called electronic commutation assembly which based on Hall Effect. Rotor speed positioning measured at 60 degree used to feed the current into stator winding via Voltage Source Inverter (VSI) [2]. Typically speed control of BLDC motor established on PWM (Pulse Width Modulation) is used. The PF (Power Factor) disturbance occurred due to Capacitor as it draws 70-80% of current supplied with THD (Total harmonic Distortion) which lead to exceed the international power quality criteria (IEC 6100-3-2) [3]. In previous decade many researchers have suggested different approaches for power factor correction convertors of BLDC motors. The suggested convertors typically operate in both intervals (Continues Conduction Interval) CCM and Discontinues Conduction

Interval (DCM). There is tradeoff between stress on converter and power rating depends on interval of operation.

For class A application (<16 A, <600 W) for mainly household applications high PF (Power Factor) and low THD is required according to international power quality standards. According to pervious literature the power quality improvement obtained using conventional boost PFC AC-DC convertor [4]. In which a constant DC link voltage is maintained at feed of VSI and PWM based current control is used for speed control. There is tradeoff between high switching frequencies (9-20 kHz) of inverter and switching losses as a high switching frequency normally increases the switching losses. Madani, S.M. [5] has been suggested four switch configuration with low cost with trade of as extra PWM switching of all switches at VSI which leads to high switching losses.

The active rectifier configuration in front of VSI for BLDC drive has been suggested in [6]. This model requires higher number of sensors resulting higher cost and complicated control.

Singh, S. [7] has been suggested similar model with front end Cuk convertor for PFC of BLDC motor. This method is use CCM (Continues Conduction Interval) of Cuk convertor which control voltage at DC-link and control PFC of high power drives.

BC (Bridgeless Configuration) of SEPIC and buck-boost convertors has been suggested in [8]. Advantages of the suggested model is in terms of reduced losses and the disadvantage is the cost in terms of large number of required active and passive elements.

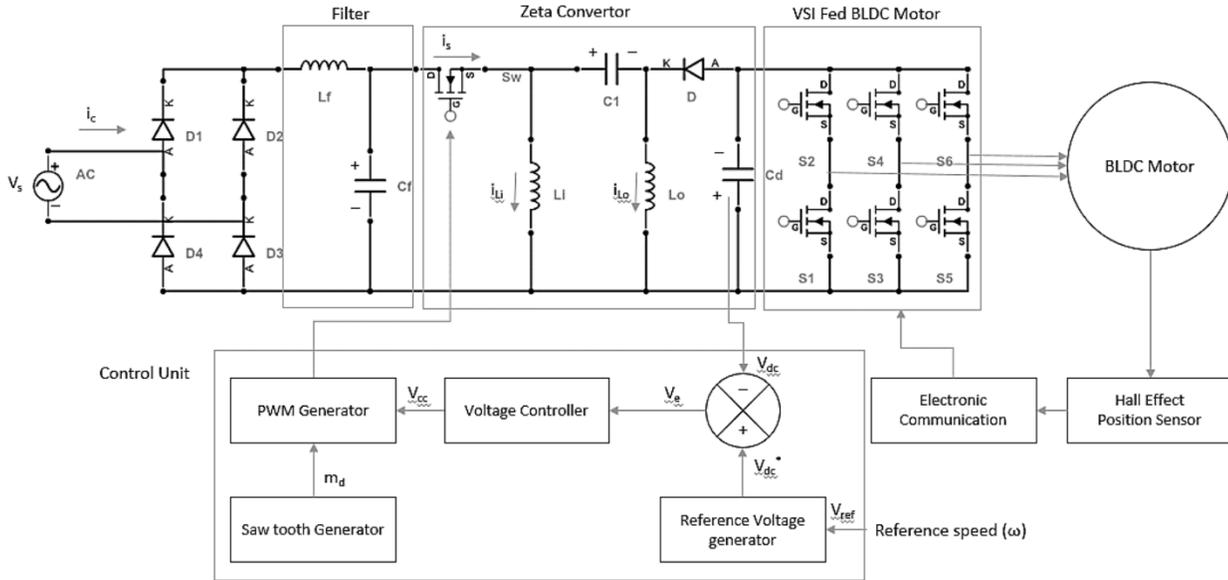


Fig 1 Model for PFC Zeta DC Motor Converter Fed Brushless DC Motor

A Zeta Converter PF pre-regulator has been widely used and it has gained reputation due to its quick dynamic performance and relatively better with light load circumstances [9]. It operates in CCM that requires a three sensor with two control loop which is costly and recommended for high power applications.

A altered Zeta converter as PF regulator is , and its applications for low cost BLDC drive is investigated in this paper.

**II. Anticipated Zeta Converter fed BLDC drive**

The suggested zeta converter arrangement follows inverter in front of BLDC drive is displayed in Fig 1.

The controlled DC voltage of inverter is used to control the speed of BLDC drive. The pre-regulated power factor improved zeta converter is intended to work in DICM (discontinuous inductor current interval). The voltage follower method is used for PFC Zeta converter to operate in DCIM which requires only one sensor for the control of DC voltage. Thus the switching of inverter for electronic commutation is on fundamental frequency that offers the reduction of losses in VSI. The suggested model for zeta converter is designed and simulated in Matlab for enhanced power factor for extensive range of speed control. The results of suggested drive are observed for different supply voltages and it's obtain power factor is acceptable under IEC 61000-3-2.

**III. Suggested Zeta converter operation**

The suggested model is designed to work in discontinuous inductor conduction interval such that there is discontinuity in conduction of output inductor \$L\_o\$ in a complete cycle. Four intervals of conduction (A, B, C, D) are displayed in fig 1.

**A. Interval A**

Interval A operation is displayed in fig 2, when the switch \$S\_w\$ is turned on, current passed through the energy storing elements and so energy stored in inductors (\$L\_i, L\_o\$) and capacitor (\$C\_1\$). Storing in energy raised the currents in respect inductivectors (\$L\_i, L\_o\$) and raised voltages across Capacitor (\$C\_1\$). As displayed in fig 2, the midway capacitor \$C\_1\$ is charged in negative direction whereas diode \$D\$ is turned

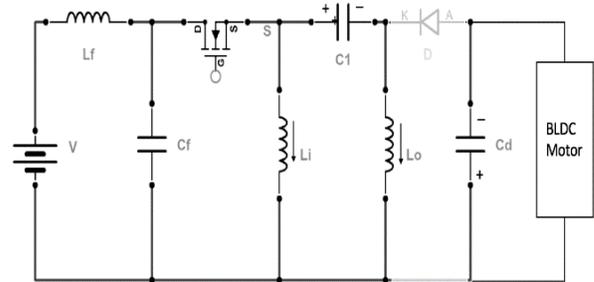


Fig 2 Interval A

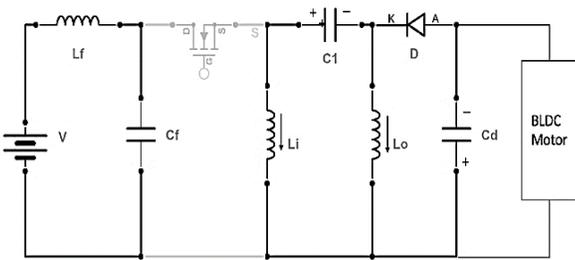
off and the Capacitor \$C\_d\$ delivers energy to the load. As the Capacitor releases its energy, voltages across \$C\_d\$ also decreases.

Second interval of interval A operation is just similar to previous operation with inverse polarity of midway capacitor \$C\_1\$. When the switch \$S\_w\$ is turned on, currents \$i\_{L\_i}, i\_{L\_o}\$ and voltages across the midway capacitor \$C\_1\$ increasing continuously. With respect to corresponding duty cycle, Interval A complete operation constitutes 15 to 25% of switching time period.

**C. Interval B**

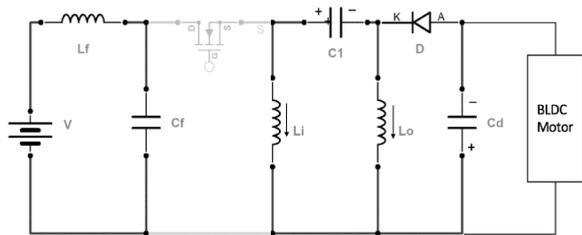
In this interval when switch  $S_w$  is turned off, discharging path for  $C_1$  through diode D is turned on so midway capacitor  $C_1$  start to discharge whereas the Capacitor  $C_d$  now start to charge through diode D. voltages across  $C_d$  and current through  $L_i$  increases whereas voltage across  $C_1$  and current through  $L_o$  decreases. Direction of currents and polarities of voltages are displayed in fig 3. Change the current and voltages in interval B. Current passing through diode D is equal to sum of total currents passing through inductors ( $L_i$  and  $L_o$ ). Discharging of midway capacitor  $C_1$  and charging of capacitor  $C_d$  becomes to end when both the capacitors maintain equal potential such that diode  $D_1$  becomes open

**D. Interval C**



**Fig 3 Interval B**

interval the voltages across the capacitor  $C_1$  becomes less than the voltage across capacitor  $C_d$  which turns on the diode D. With short of discharging path, midway capacitor  $C_1$  discharges through inductor  $L_i$  and  $L_o$  as displayed in fig 4. Inductor  $L_o$  discharges continuously to Capacitor through diode D. Due to discharging the value of current through inductor  $L_o$  decreases continuously also the current of inductor  $L_i$  increases in interval C. This interval of operation ends as the current of output inductor  $L_o$  come to be zero.



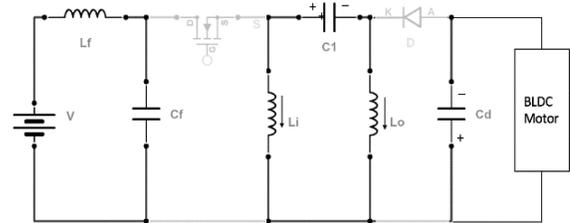
**Fig 4 Interval C**

**E. Interval D**

For the interval of discontinuous conduction, the parameters designed for both inductors are different such that  $L_i$  is much higher as compared to  $L_o$  which guarantees the discontinuous operation interval in mentioned settings so  $L_o$  discharges completely in a cycle. In this interval of operation, the midway capacitor discharges continuously so that voltages across  $C_1$  decreases whereas the current through  $L_i$  increases continuously. The diode D remain turned off and the current through  $L_o$  becomes equal to the current through  $L_i$  in this interval. During this operation the Capacitor  $C_d$  supplies the energy to drive and operation becomes to end when  $C_1$

discharged completely.

The second interval of operation in its parental interval D is next step of aforementioned operation when  $C_1$  becomes fully discharged it starts charging again in opposite direction. For charging operation, the current is supplied through inductor  $L_i$  and the capacitor  $C_1$  charged to its value. With the charging of  $C_1$  the voltages across  $C_1$  increases continuously whereas the current through  $L_i$  decreases with increase of  $V_{dc}$  as displayed in fig 3. The diode D continue in its off



**Fig 5 Interval D**

conduction interval and the capacitor  $C_d$  supplies energy to the output drive. The operation interval D constitutes 50 to 70% time of complete switching period. Complete interval D operation is displayed in fig 5.

**IV. Design of improved zeta converter**

For the operation of suggested converter, the ideal selection inductors ( $L_i$  and  $L_o$ ), centered and capacitors ( $C_1$  and  $C_d$ ) the inductor and capacitor for DC filter ( $C_f$  and  $L_f$ ) are necessary for required action. Some assumption are made for the suggested converter are as follow:

- 1) The PFC converter has ideal components such that there is no loss output and input powers are equal.
- 2) The resistance of inductor are assumed to be zero such that there is no saturation in the inductors.
- 3) Midway and capacitor  $C_d$  are supposed to be ideal such that they have zero equal resistance.
- 4) The switching periods are considered to be zero as relative to time constant of capacitors and inductor.

The converter have to work in DCIM so that current through inductor come to be discontinuous in all switching duration. The DC link voltage are controlled by PI controller such that  $V_{dcmax}=200V$  and  $V_{dcmin}=50V$ . For the worse case of duty cycle in which supply voltage is minimum inductor is designed to operate in discontinuous interval. The power factor convertor in designed for 350W BLDC motor.

$$V_{supply} = V_{max}(2\pi f_L t) = 220\sqrt{2} \sin(314t) V \quad (1)$$

Peak input voltage  $V_m$  and  $f_L$  is 50 Hz the line frequency.

The instantaneous voltage across DBR is given as

$$V_i(t) = |V_{max} \sin \omega t| = |220\sqrt{2} \sin(314t)|V \quad (2)$$

The buck boost configuration of zeta converter are as

$$V_{dc} = \frac{D}{1-D} V_i(t) \quad (3)$$

Where D is duty ratio, its depend on the input DBR voltage and Capacitor voltage The value of duty cycle is obtained by substituting and rearranging equation (2) and (3) as

$$D(t) = \frac{V_{dc}}{V_i(t) + V_{dc}} = \frac{V_{dc}}{V_m \sin \omega t + V_{dc}} \quad (4)$$

The  $P_i$  power transmitted and the DC voltage as the function of  $V_s$  as the speed of BLDC drive is controlled by changing the DC voltage fed to the inverter, since the  $R_i$  of converter is give as

$$R_{in} = \frac{\{V_{in}(t)\}^2}{P_i} = \frac{V_s^2}{p_i} \quad (5)$$

Therefore the  $R_{in}$  value depend upon the DC link voltage and supply voltage.

For the rated power  $P_{max} = 350W$  and the supply voltage the  $V_s = 85v$  the value of  $R_{in}$  is  $20.64\Omega$  and the maximum value as the  $V_{dc} = 50V$  and Power  $87.5W$  with  $V_s = 270V$  is  $1041.43 \Omega$ . Hence the  $R_{in}$  varies from  $20.64\Omega$  to  $1041.43 \Omega$ .

### A. Design of inductor $L_i$

The  $\eta$  is the current ripple allowed by inductor, at the rated conditions  $V_{dc} = 200V$  and the minimum value of  $V_s$  maximum current is obtained, hence the  $L_i$  is designed for minimum value of  $V_s$  as [10].

$$\begin{aligned} L_i &= \frac{1}{\eta f_s} \left( \frac{V_s^2}{P_{mx}} \right) \left( \frac{V_{dc mx}}{\sqrt{2} V_s mn + V_{dc}} \right) \quad (6) \\ &= \frac{1}{0.2 \times 20000} \left( \frac{85^2}{350} \right) \left( \frac{200}{85\sqrt{2} + 200} \right) \\ &= 3.22 \text{ mH} \end{aligned}$$

The value of  $L_i$  is  $3.22 \text{ mH}$  for the 20 % amount of ripple current.

### B. Design of $L_o$

The output inductor  $L_o$  designed as

$$\begin{aligned} L_{oc} &= \frac{V_{dc} (1 - D(t))}{2i_{Lo}(t) f_s} = \frac{V_{dc} D(t)}{2I_{in}(t) f_s} = \frac{R_{in} V_{dc} D(t)}{2V_{in}(t) f_s} \\ &= \left( \frac{V_s^2}{P_i} \right) \frac{V_{dc}}{2V_{in}(t) f_s} \left( \frac{V_{dc}}{V_i(t) + V_{dc}} \right) \quad (7) \end{aligned}$$

The worst case if the input voltage is  $V_{dc} = 50V$  then the value of  $L_o$  as

$$\begin{aligned} &= \left( \frac{V_s^2}{P_i} \right) \frac{V_{dc min}}{2\sqrt{2} V_{in min}(t) f_s} \left( \frac{V_{dc min}}{\sqrt{2} V_i min(t) + V_{dc min}} \right) \\ &= \left( \frac{85^2}{70} \right) \frac{50}{2\sqrt{2} \times 85 \times 20000} \left( \frac{50}{85\sqrt{2} + 50} \right) \\ &= 315.3 \mu H \end{aligned}$$

The value of the  $L_o$  should be less than the critical value as a result the chosen value is  $70 \mu H$  [5].

### C. Design of $C_1$

The value of the midway capacitor  $C_1$  in common conduction interval for k% ripple voltages is given as [3].

$$\begin{aligned} C_1 &= \frac{V_{dc} D(t)}{k V_{C1}(t) f_s R_L} \\ &= \frac{V_{dc}}{k \{V_{dc} + V_{in}(t)\} f_s (V_{dc}^2 / P_i)} \left( \frac{V_{dc}}{V_i(t) + V_{dc}} \right) \quad (8) \\ &= \frac{P_i}{K f_s (V_{in}(t) + V_{dc})^2} \end{aligned}$$

Therefore the maximum value of supply voltage  $V_s$  and DC link voltage  $V_{dc}$  are used for the value of midway capacitor  $C_1$

$$\begin{aligned} &= \frac{P_{max}}{K f_s (V_s mx(t) + V_{dc mx})^2} \\ &= \frac{350}{0.1 \times 20000 (270\sqrt{2} + 200)^2} = 0.516 \mu F \end{aligned}$$

Where the value of K is selected as 10% of the minimum voltage on capacitor  $V_{C1}$ . Therefore the value of capacitor  $C_1$  is selected as  $0.68 \mu F$  for common interval conduction. The commonly used capacitors for this type of application must have low equivalent resistance which make them suitable for high frequency and high surge current applications.

### D. Design of capacitor $C_d$

The value of Capacitor  $C_d$  as has suggested in [9].

$$C_d = \frac{I_{dc}}{2\omega \Delta V_{dc}} = \frac{P_i}{2\omega \delta V_{dc}^2} \quad (10)$$

Where  $\delta$  the voltage ripple and  $I_{dc}$  is the current through cd, therefore the value of  $C_d$  is calculated for minimum  $V_{dc}$  (DC link Voltage) as

$$C_d = \frac{P_{min}}{2\omega\delta V_{dc min}^2}$$

$$= \frac{70}{2 \times 314 \times 0.04 \times 40^2} = 1741.6 \mu F$$

The capacitor value should take higher than above value because the ripple voltages should be less than 4% even for minimum value of  $V_{dc}$ . So the selected value is 2000  $\mu F$  for this application. In this application capacitor has to operate with high current and low frequency switching that why best suited capacitor is electrolytic.

### E. Design of filter capacitor $C_f$ and inductor $L_f$

Radzoun. [8] Calculated the value of  $C_f$  and  $L_f$  as

$$C_f < C_{max} = \frac{I_{peak}}{\omega_L V_{peak}} \tan(\phi)$$

Table 1 Simulated results for the suggested drive, varying speed.

$$= \frac{\left(\frac{350\sqrt{2}}{220}\right)}{314 \times 220 \sqrt{2}} \tan(1^\circ) = 401.98 nF$$

Where the  $I_{peak}$ ,  $V_{peak}$  and  $\phi$  are the peak supply current , peak voltage ,and the angle between the supply current and voltages respectively. The value that is selected for this application is 330 nF.

$$L_f = L_{req} + L_s \Rightarrow \frac{1}{4\pi^2 f_c^2 C_f} \quad (11)$$

$$= L_{req} + 0.04 \left(\frac{1}{\omega_L}\right) \left(\frac{V_s^2}{p_0}\right) \Rightarrow L_{req}$$

$$= \frac{1}{4\pi^2 f_c^2 C_f} - 0.04 \left(\frac{1}{\omega_L}\right) \left(\frac{V_s^2}{p_0}\right) = 1.57mH$$

Where  $f_c$  is the cut off frequency selected as

$$f_{sw} < f_c < f_L$$

Therefore, the value of  $f_c$ , is taken as  $f_{sw}/10$  to achieve electronic commutation at fundamental frequency for switching of voltage source inverter.

### V. Suggested BLDC drive simulated results

The results for the suggested drive are simulated in MATLAB-Simulink environment for improved performance over a wide speed range. Some factors related to BLDC drive

and zeta converter i.e. Switches current and voltage ( $v_{sw}$  and  $i_{sw}$ ), centered capacitor voltage ( $V_{c1}$ ), inductor currents ( $i_{L1}$  and  $i_{L0}$ ), stator current ( $i_a$ ), electromagnetic torque ( $T_e$ ), speed ( $\omega$ ), DC link voltage ( $V_{dc}$ ), supply current ( $i_s$ ) and supply

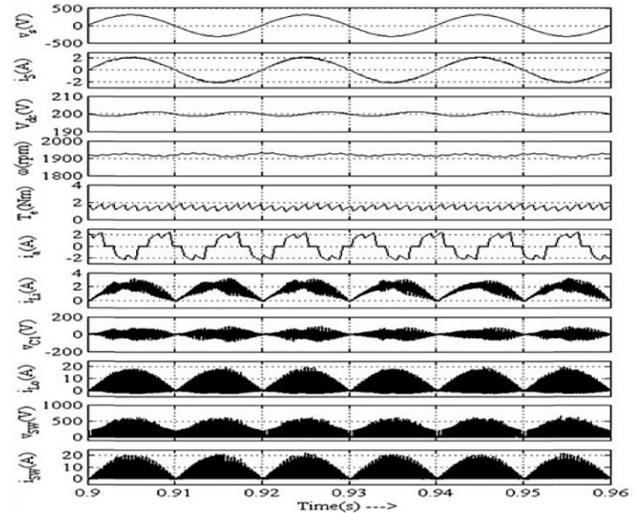


Fig 6 Steady state results of BLDC drive when Vs 220V and Vdc 200V

voltages ( $V_s$ ) are explained the performance of model. Further to explain the enhanced power quality of the drive

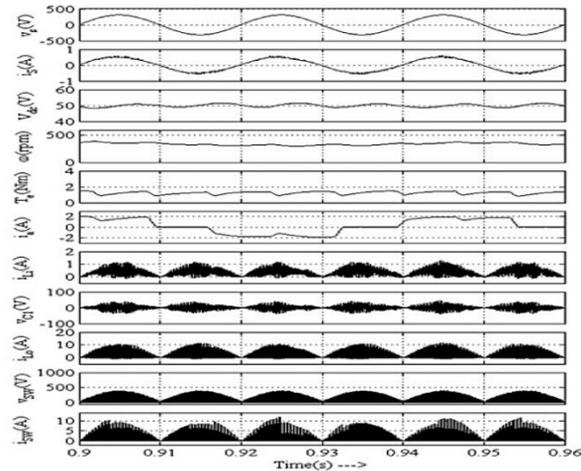


Fig 7 Steady state results of BLDC drive at Vs 220V and Vdc 50V

PF (power factor) and THD of  $i_s$  are also observed. Suggested drive simulated results are as follow.

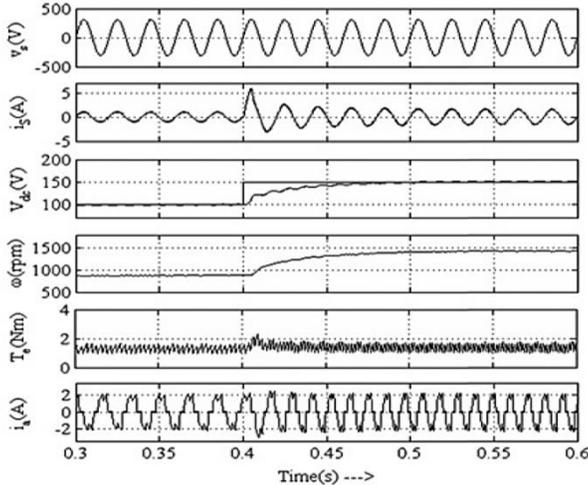


Fig 8 Changing  $V_{dc}$  from 100 to 150V

**A. BLDC drive in steady state**

The results obtained at steady state conditions at rated torque with  $V_{dc}$  200V and 50V are in figs 6 and b respectively. The supply voltage and supply current obtain are in phase which demonstrate the PF is unity at AC main. A discontinuous current in inductor  $i_{L_o}$  and a continuous current in  $i_{L_o}$  are obtained which shows the DCIM operation of Zeta. And the obtain THD of  $i_s$  is within the limits of IEC 61000-3-2 [3]. The results of the suggested drive are tabulated in Table 1.

Table 1 Simulated results of suggested drive, varying speed

$V_{dc}$ , V	RPM	THD% of $i_s$	PF	$I_s$ , A
50	350	5.6	0.84	0.29
80	700	3.6	0.85	0.56
110	910	2.8	0.87	0.83
140	1330	2.6	0.91	1.02
170	1710	2.45	0.93	1.31
200	1950	2.3	0.93	1.46

Table 2 Simulated results at different supply voltages

$V_s$ , V	THD% of $i_s$	PF	$I_s$ , A
170	2.1	0.82	1.94
190	2.13	0.83	1.72
210	2.63	0.86	1.56
230	2.69	0.90	1.45
250	2.75	0.91	1.39
270	2.92	0.94	1.22

**B. Results at different supply voltages**

For the complete range of supply the improved power quality is displayed in table 2.

**C. Dynamic result of suggested drive**

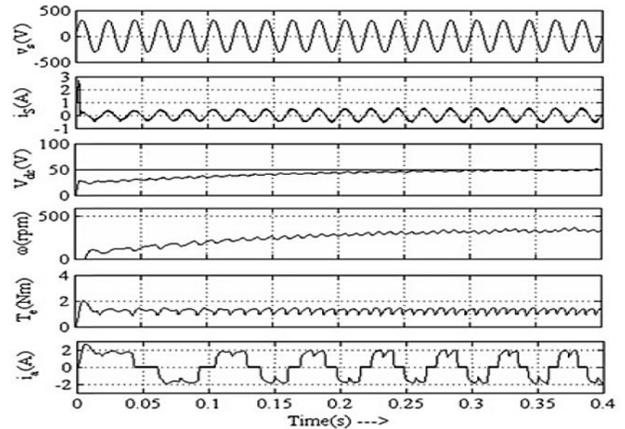


Fig 9 Dynamic result of BLDC drive at  $V_{dc}$  50V

The dynamic result of drive at initial conditions and speed control is displayed in the fig 8 and 9, respectively. The performance when the starting of BLDC drive at 50V is displayed in fig 8. Further the performance of drive during step change in  $V_{dc}$  are displayed in fig 9. The control of  $V_{dc}$  limited transient stator and supply current during speed control and starting.

**CONCLUSION**

For the low power applications, the power factor improved zeta converter in front of BLDC drive is very effective and cheap solution. The suggested BLDC drive has been schemed for the controlled speed of wide range with enhanced power feature at AC source. A voltage follower topology is used to control the drive speed by varying the DC voltages at the input of inverter. This technique enables the switching of voltage source inverter on fundamental frequency for attaining an electronic commutation to minimize the switching losses. An improved zeta converter scheme work in discontinuous current mode leads a voltage follower topology to control the DC output. The results of the BLDC drive has been assessed for different input voltages and controlled speed.

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