

# ONLINE PARAMETER ESTIMATION OF PERMANENT MAGNET SYNCHRONOUS MOTOR BY ACTIVE IDENTIFICATION

Iman Yousefi, Mahmood Ghanbari\*

Department of Electrical Engineering, AliAbad Katoul Branch, Islamic Azad University, AliAbad Katoul, Iran.

\*Corresponding author: Mahmood Ghanbari, Email: [mmm\\_gh\\_53@yahoo.com](mailto:mmm_gh_53@yahoo.com), Fax: +98 1732158891

**ABSTRACT:** *Online active identification method is used for parameter estimation due to fast variations of parameters in permanent magnet synchronous motor (PMSM). This method has the ability to estimate the parameters in a certain range of time. In order to implement the estimator, linear regression form is heuristically obtained by non-linear model of discrete mode. The proposed method is then compared to recursive least squares estimator for evaluation. The results show superiority of the proposed method in terms of speed and accuracy.*

**Keywords:** Active identification, Orthogonal projection algorithm, Non-linear model of Permanent Magnet Synchronous Motor, Linear regression form, Parameters estimation

## Nomenclature

### Constant

$R$ : stator resistance

$p$ : pole-pairs

$\Phi_f$ : magnet flux linkage

$J$ : Inertia coefficient

$L_d$ : direct and quadrature inductances of Park transformation

$L_q$ : direct and quadrature inductances of Park transformation

$\theta_1$ : parameter vector form 1

$\theta_2$ : parameter vector form 2

### Variables

$i_q$ : Park transformation currents

$i_d$ : Park transformation currents

$\Omega$ : Rotor angular speed

$\delta$ : rotor angular position

$i_m$ : nominal current

$\phi_1$ : estimator vector Form 1

$\phi_2$ : estimator vector Form 2

$y_1$ : output Form 1

$y_2$ : output Form 2

$p$ : covariance Matrix

$L_2$ : second norm of parameter estimation error vector

$J$ : normalized residue

### Indices

$k$ : step sample time in discrete time

$t$ : time(sec)

## 1. INTRODUCTION

Regarding the increase in complexity of power systems, there is a need for more accurate model to achieve physical parameters. In recent years, permanent magnet synchronous motors are widely used in industrial applications. Such kind of motor has gained too much attention due to some excellent features like high efficiency, compact structure, robust construction, high power, high torque to inertia ratio, high torque density capability and simpler controller comparing to induction and DC motors [1-7]. Therefore, controlling such motors is very important. Physical parameters of these non-linear time variable motors are affected by different factors

like temperature, mechanical vibrations, loading conditions, longing of ageing and environmental factors [8-9]. These variations lead to parametric uncertainty in system and affect the selection of model and parameter estimation when one is going to design its controller [10-11]. Different methods have been used to estimate the parameters of PMSM. It is often tried to identify the parameters in online condition to better control the system. Some factors affect the parameter estimation like speed of convergence, accuracy, initial estimation of parameters and noise conditions. Every identification algorithms cover one or more superiority factors in parameter estimation with regards to their features. Extended Kalman filter and reference model which cover speed factor and convergence accuracy, neural networks with learning capability and , recursive least squares robust to noise are some of the methods illustrated in the control literatures.[12-19]

One of the online methods to identify and estimate the non-linear systems is the active identification method[30] which is used for identification of synchronous generator power system [20] and covers all the above mentioned factors. In this study, active identification method is applied to the non-linear model of PMSM without any simplification or linearization in order to estimate the physical parameters.

The proposed estimator is described in section 2. In section 3, the proper model of system and changing it into linear regression form for implementing the estimator is presented. After that, the results of the proposed estimator are compared with the results of least square estimator in simulation section. Finally, the paper is concluded in section 5.

## 2. Description of active identification method

One of the methods for parameter estimation is the orthogonal projection algorithm. This method tries to produce orthogonal estimator vectors by making a vector subspace that constitute the bases of this space in order to project the unknown parameter vector on this subspace [21]. The disadvantage of this algorithm is the uncertain time for completing the estimation subspace. In active identification, output is guided toward the way that these independent estimator vectors are produced by giving purposed input to the system in order to facilitate the estimation in a certain amount of time [22]. This estimator would be useful for a system like PMSM in which its parameters are varied by different factors.

Orthogonal projection algorithm is a linear equations method to linear regression form which is given in equation (1).  $y$  is the output of scalar,  $\hat{\phi}$  estimator vector,  $\theta$  unknown parameter and  $e$  noise in the system.

$$y[t] = \phi^T [t] \hat{\theta} + e[t] \quad (1)$$

Considering this equation, OPA is started by using equations (2) and with an initial estimation of parameters  $\hat{\theta}_0$  and covariance identity matrix  $P_0$  [23].

if  $\phi_{t-1}^T P_{t-1} \phi_{t-1} \neq 0 \Rightarrow$

$$\begin{cases} \hat{\theta}_t = \hat{\theta}_{t-1} + \frac{P_{t-1} \cdot \phi_{t-1}}{\phi_{t-1}^T \cdot P_{t-1} \cdot \phi_{t-1}} \cdot [y[t] - \hat{\theta}_{t-1}^T \cdot \phi_{t-1}] \\ P_t = P_{t-1} + \frac{P_{t-1} \cdot \phi_{t-1} \cdot \phi_{t-1}^T \cdot P_{t-1}}{\phi_{t-1}^T \cdot P_{t-1} \cdot \phi_{t-1}} \end{cases} \quad (2)$$

if  $\phi_{t-1}^T P_{t-1} \phi_{t-1} = 0 \Rightarrow \hat{\theta}_t = \hat{\theta}_{t-1}, P_t = P_{t-1}$

The two conditions in (2) investigate the orthogonal situation of estimator vector. If the estimator vector is independent and linear toward its previous, parameter estimation and covariance matrix are updated, otherwise previous values of covariance and parameters are maintained.

Active identification method is formed by adding input selection to the OPA, at first system is with rank  $n$ , then input is cut and output is sample. Estimator vector  $\hat{\phi}_t$  in each sample  $t$  is investigated. If it can form a basic vector for estimation subspace, the estimator performs a new estimation of the parameters then waits until the measurement of the next sample, otherwise previous values are kept. Then investigation process and pre-calculation of output (regarding the features of orthogonal projection) would continue until the sample  $(t+n)$ . If an independent vector is formed based on dynamics of system until sample  $(t+n)$ , we would wait, otherwise for producing independent estimator vectors in samples  $(t+n+1)$ , an input is needed for system to produce an output in order to produce independent linear estimator vector with respect to previous vectors. This process would continue until completion of bases for estimation subspace.  $n$  samples are needed to do this. Finally, active identification algorithm ends at most with  $2nr$ . The stages of algorithm are described in detail as:

In active identification method, applying an input for speeding up the convergence of parameters is performed on several sampling time. Therefore, at first inputs are considered zero and if needed, purposed input is applied to the system.

Stage zero: initializing the parameters vectors  $\hat{\theta}_0$ , square matrix  $P_0$  and iteration variable  $L=0$

First stage: sampling is performed from input and output until  $t=n-1$  and estimator vector  $\hat{\phi}$  is formed and up to this time it

is considered  $\hat{\theta}_t = \hat{\theta}_0$  and  $P_t = P_0$

Second stage: forecast time  $tp$  is set to  $n-1$

Third stage: vectors  $\hat{\phi}_{tp}$  are calculated and the orthogonal condition of estimator vector is investigated ( $\hat{\phi}_{tp}^T P_{t-1} \hat{\phi}_{tp} \neq 0$ ), if condition is fulfilled, a step is added to  $tp$  ( $tp=tp+1$ ), then initialize  $t=tp$  and going to the next stage, otherwise going to seventh stage

Fourth stage: performing the sampling of output  $y(t)$  at instant  $t$

Fifth stage: updating the covariance matrix ( $p_t$ ) and parameter vector ( $\hat{\theta}_t$ ) based on equation (2) and  $L=L+1$

Sixth stage: if  $L$  is equal to the dimension of parameters vector ( $\dim(\theta)=L$ ), estimation is finished and  $\hat{\theta}_t = \theta$  and covariance matrix is equal to zero, otherwise going to third stage

Seventh stage: output is pre-calculated at  $(tp+1)$  (to produce a new base for estimation subspace)

$$y(tp+1) = \hat{\phi}_{t-1}^T \theta \quad (3)$$

Eighth stage: one step is added to  $tp$  ( $tp=tp+1$ ), if  $tp < t+n$  going to third stage otherwise going to next stage

Ninth stage: an accidental vector with the same dimension of the number of input for system for  $u(t)$  (to determine an input that goes  $y(t+n+1)$  toward a new base))

Tenth stage: if the condition is not met  $\hat{\phi}_{tp}^T P_{t-1} \hat{\phi}_{tp} \neq 0$ , returning to ninth stage, otherwise a step is added to  $tp$  ( $tp=tp+1$ ) and  $t=tp$  and going to fourth stage.

### 3. Linear regression form of PMSM

The selected model for PMSM is a fourth rank model to be near to reality and considering the dynamics of the system [24-26].

$$\begin{aligned} \frac{d\delta}{dt} &= \Omega \\ \frac{d\Omega}{dt} &= \frac{p}{J} \Phi_f i_q - \frac{1}{J} T_e \\ \frac{di_q}{dt} &= -\frac{R}{L_q} i_q - p\Omega i_d - p \frac{1}{L_q} \Phi_f \Omega + \frac{1}{L_q} v_q \\ \frac{di_d}{dt} &= -\frac{R}{L_d} + p\Omega i_q + \frac{1}{L_d} v_d \end{aligned} \quad (4)$$

$\delta$  is power angle,  $\Omega$  angular velocity,  $i_d$  and  $i_q$  Park's transformation currents of state variables of the system,  $R$  stator resistance,  $L_d$  and  $L_q$  Parks' transformation inductance,  $p$  number of pole-pairs,  $\Phi_f$  flux linkage,  $J$  inertia coefficient of physical parameters and  $T_e$  electromagnetic torque.

The aim of this part of the paper is to rewrite this non-linear model as linear regression form considering availability of power angle ( $\delta$ ) which this variable is selected as desired output for linear regression form. State space model will be according to equation (6) using equation (5) [27] and discretization based on  $(\dot{x} = [x(t+T_s) - x(t)]/T_s)$  where  $T_s$  is sampling time:

$$\begin{cases} \dot{i}_d = i_m \cos(\delta) \\ \dot{i}_q = i_m \sin(\delta) \end{cases} \Rightarrow \begin{cases} \dot{i}_d = i_m \cos(x_1) \\ \dot{i}_q = i_m \sin(x_1) \end{cases}$$

$$T_e = 1.5(L_d - L_q) \dot{i}_d i_q \tag{5}$$

$$\begin{cases} x_1[k + T_s] = x_1[k] + T_s x_2[k] \\ x_2[k + T_s] = x_2[k] + T_s \left( \frac{1.5P\Phi_f}{J} \right) x_3[k] + T_s \left( \frac{1.5(L_d - L_q)}{J} \right) x_3[k] x_4[k] \\ x_3[k + T_s] = T_s \left( \frac{-\Phi_f P}{L_q} \right) x_2[k] + T_s \left( \frac{-R}{L_q} \right) i_m \sin(x_1[k]) + T_s/L_q u_1[k] \\ \quad + T_s \left( -p \frac{L_d}{L_q} \right) i_m \cos(x_1[k]) x_2[k] + i_m \sin(x_1[k]) \\ x_4[k + T_s] = i_m \cos(x_1[k]) + T_s \left( \frac{-R}{L_d} \right) i_m \cos(x_1[k]) + \frac{T_s}{L_d} u_2 \\ \quad + T_s \left( p \frac{L_q}{L_d} \right) i_m \sin(x_1[k]) x_2[k] \end{cases} \tag{6}$$

In (6), all state variables are rewritten to linear regression form based on the first variable i.e. power angle  $x_1$ . Physical parameters are estimated as factors due to multiplying the physical parameters with another. At the end of estimation, to separate the physical parameters, complex non-linear equations have to be solved. Therefore, to avoid solving non-linear equations, equation (6) is rewritten into two linear regression forms based on variable ( $x_1$ ) in order to obtain the parameters using simple mathematical relations.

**3.1. First form**

The second state variable of equation (6) can be rewritten by using equation (5) as below:

$$x_2[k + T_s] = x_2[k] + T_s \left( \frac{1.5P\Phi_f}{J} \right) x_3[k] + T_s \left( \frac{1.5(L_d - L_q)}{J} \right) \frac{i_m^2}{2} \sin 2(x_1[k]) \tag{7}$$

By shifting forward in equation (7) and putting  $x_3[k + 1]$  in it from equation (6) and substituting  $T_s = 1$ :

$$\begin{aligned} x_2[k + 2] &= x_2[k + 1] + \left( \frac{1.5(L_d - L_q) i_m^2}{2J} \right) \sin 2(x_1[k + 1]) \\ &+ \left( \frac{1.5P\Phi_f}{J} \right) \left( \frac{-\Phi_f P}{L_q} \right) x_2[k] + \left( \frac{1.5P\Phi_f}{J} \right) \left( \frac{-R}{L_q} \right) \sin(x_1[k]) + \left( \frac{1.5P\Phi_f}{L_q J} \right) u_1[k] + \\ &\left( \frac{1.5P\Phi_f}{J} \right) \left( -p \frac{L_d}{L_q} \right) \cos(x_1[k]) x_2[k] + \left( \frac{1.5P\Phi_f i_m}{J} \right) \sin(x_1[k]) \end{aligned} \tag{8}$$

Equation (8) is rewritten in terms of load angle by using the relation between first and second state variables:

$$\begin{aligned} x_1[k + 3] - x_1[k + 2] &= x_1[k + 2] - x_1[k + 1] + \\ &\left( \frac{1.5P\Phi_f}{J} \right) \left( \frac{-\Phi_f P}{L_q} \right) (x_1[k + 1] - x_1[k]) + \left( \frac{1.5P\Phi_f}{J} \right) \left( \frac{-R}{L_q} \right) \\ &\sin(x_1[k]) + \left( \frac{1.5P\Phi_f}{L_q J} \right) u_1[k] + \left( \frac{1.5P\Phi_f}{J} \right) \left( -p \frac{L_d}{L_q} \right) \\ &\cos(x_1[k]) (x_1[k + 1] - x_1[k]) + \left( \frac{1.5P\Phi_f i_m}{J} \right) \sin(x_1[k]) + \left( \frac{1.5(L_d - L_q) i_m^2}{2J} \right) \sin 2(x_1[k + 1]) \end{aligned} \tag{9}$$

The above equation is rewritten to the below form by defining new variables:

$$\begin{aligned} y_1[k] &= A_1 y_{11} + A_2 y_{12} + A_3 y_{13} + A_4 y_{14} + A_5 y_{15} \tag{10} \\ A_1 &= \left( \frac{1.5P\Phi_f}{J} \right) \left( \frac{-\Phi_f P}{L_q} \right) & A_2 &= \left( \frac{1.5P\Phi_f}{J} \right) \left( \frac{-R}{L_q} \right) + \left( \frac{1.5P\Phi_f i_m}{J} \right) \\ A_3 &= \left( \frac{1.5P\Phi_f}{L_q J} \right) & A_4 &= \left( \frac{1.5P\Phi_f}{J} \right) \left( -p \frac{L_d}{L_q} \right) \\ A_5 &= \left( \frac{1.5(L_d - L_q) i_m^2}{2J} \right) \end{aligned}$$

$$\begin{aligned} y_{11} &= (x_1[k + 1] - x_1[k]) & y_{12} &= \sin(x_1[k]) \\ y_{13} &= u_1[k] & y_{14} &= \cos(x_1[k]) (x_1[k + 1] - x_1[k]) \\ y_{15} &= \sin 2(x_1[k + 1]) & y_{16} &= x_1[k + 3] - 2x_1[k + 2] + x_1[k + 1] \end{aligned}$$

Finally a non-linear model of PMSM is written to common linear regression form considering equation (10) without any linearization in which  $A_1, \dots, A_7$  are factors that are obtained from multiplying physical parameters of the system and  $y_{11}, \dots, y_{15}$  are variables that are composed of non-linear functions, input and output.

Equation (10) can be written to the linear regression matrix: In equation (10),  $\phi_1$  is estimator vector for first regression form and  $\theta_1$  parameters vector related to this form.

$$y_1[k] = \phi_1^T \theta_1 \tag{11}$$

$$\begin{aligned} \phi_1 &= [y_{11} \quad y_{12} \quad y_{13} \quad y_{14} \quad y_{15}]^T \\ \theta_1 &= [A_1 \quad A_2 \quad A_3 \quad A_4 \quad A_5] \end{aligned}$$

**3-2- Second form**

The second state variable of equation (6) can be rewritten by using equation (5) as below:

$$\begin{aligned} x_2[k + T_s] &= x_2[k] + T_s \left( \frac{1.5P\Phi_f i_m}{J} \right) \sin(x_1[k]) + T_s \left( \frac{1.5(L_d - L_q) i_m}{J} \right) \sin \\ &(x_1[k]) x_4[k] \end{aligned} \tag{12}$$

By shifting forward in equation (12) and putting  $x_3[k + 1]$  in it from equation (3) and substituting  $T_s = 1$ :

$$\begin{aligned}
 x_2[k+2] = & x_2[k+1] + \left(\frac{1.5P\Phi_f i_m}{J}\right) \sin(x_1[k+1]) + \left(\frac{1.5(L_d - L_q)i_m^2}{J}\right) \sin(x_1[k+1])\cos(x_1[t]) \\
 & + \left(\frac{1.5(L_d - L_q)i_m}{L_d J}\right) u_2 + \left(\frac{1.5(L_d - L_q)i_m^2}{J}\right) \left(\frac{-R}{L_d}\right) \sin(x_1[k+1])\cos(x_1[t]) + \\
 & \left(\frac{1.5(L_d - L_q)i_m^2}{J}\right) \left(\frac{P L_q}{L_d}\right) \sin(x_1[k+1])\sin(x_1[k])x_2[k]
 \end{aligned}
 \tag{13}$$

Equation (13) is rewritten in terms of load angle by using the relation between first and second state variables:

$$\begin{aligned}
 x_1[k+3] - x_1[k+2] = & x_1[k+2] - x_1[k+1] + \left(\frac{1.5P\Phi_f i_m}{J}\right) \sin(x_1[k+1]) + \left(\frac{1.5(L_d - L_q)i_m^2}{J}\right) \\
 & \sin(x_1[k+1])\cos(x_1[k]) + \left(\frac{1.5(L_d - L_q)i_m}{L_d J}\right) \sin(x_1[k+1])u_2 + \left(\frac{1.5(L_d - L_q)i_m^2}{J}\right) \left(\frac{-R}{L_d}\right) \\
 & \sin(x_1[k+1])\cos(x_1[k]) + \left(\frac{1.5(L_d - L_q)i_m^2}{J}\right) \left(\frac{P L_q}{L_d}\right) \sin(x_1[k+1])\sin(x_1[k])(x_1[k+1] - x_1[k])
 \end{aligned}
 \tag{14}$$

The above equation is rewritten to the below form by defining new variables:

$$\begin{aligned}
 y_2[k] = & B_1 y_{21} + B_2 y_{22} + B_3 y_{23} + B_4 y_{24} \tag{15} \\
 B_1 = & \left(\frac{1.5P\Phi_f i_m}{J}\right) \\
 B_2 = & \left(\frac{1.5(L_d - L_q)i_m^2}{J}\right) \left(1 + \left(\frac{-R}{L_d}\right)\right) \\
 B_3 = & \left(\frac{1.5(L_d - L_q)i_m}{L_d J}\right) \\
 B_4 = & \left(\frac{1.5(L_d - L_q)i_m^2}{J}\right) \left(\frac{P L_q}{L_d}\right)
 \end{aligned}$$

$$\begin{aligned}
 y_2[k] = & x_1[k+3] - 2x_1[k+2] + x_1[k+1] \\
 y_{21} = & \sin(x_1[k+1]) \quad y_{22} = \sin(x_1[k+1])\cos(x_1[k]) \\
 y_{23} = & \sin(x_1[k+1])u_2[k] \quad y_{24} = \sin(x_1[k+1])\sin(x_1[k])(x_1[k+1] - x_1[k])
 \end{aligned}$$

Finally a non-linear model of PMSM is written to common linear regression form like form NO.1 considering equation (15) without any linearization in which  $B_1, \dots, B_4$  are factors that are embedded in the physical parameters of the system and  $y_{21}, \dots, y_{24}$  are variables that are composed of non-linear functions, input and output.

Equation (15) can be written to the linear regression matrix like form NO.1:

$$\begin{aligned}
 y_2[k] = & \phi_2^T \theta_2 \tag{16} \\
 \phi_2 = & [y_{21} \quad y_{22} \quad y_{23} \quad y_{24}]^T \\
 \theta_2 = & [B_1 \quad B_2 \quad B_3 \quad B_4]
 \end{aligned}$$

In equation (11),  $\phi_2$  is estimator vector and  $\theta_2$  parameters vector related to form NO.2

### 4. Simulation

To validate and investigate the strategy of active identification method, the proposed method is implemented on a state space model of PMSM which is rewritten to linear

regression form in section 3 with specifications of Table 1.[24]

**Table (1): Parameters of the under study system**

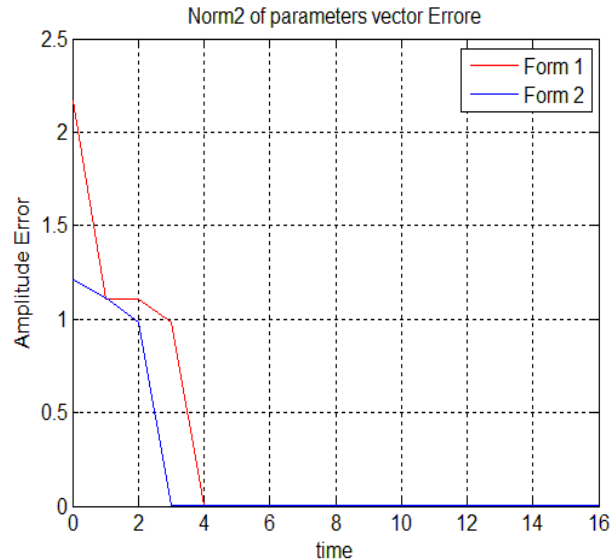
R	$L_q$	$L_d$	$\lambda_f$	j	p
2.87 $\Omega$	9 mH	7 mH	0.175mWb	8 gm <sup>2</sup>	4

To show the superiority of the proposed method, it is compared to common recursive least square estimator in terms of speed of convergence, accuracy in parameters estimation and initial estimation in noise-free situation. System is in stable mode and power angle is considered as output. Active identification method is started in parallel with the initial estimation of physical parameters in an accidental way for both of the linear regression forms explained in section 3. At first, the inputs of the system are cut, outputs are sampled and if needed, the purposed input is applied to the system based on the algorithm.

Stop criterion for identification is considered as the second norm error of parameter estimation vector according to equation (17).

$$L_2 = \|\theta - \hat{\theta}\|_2 \tag{17}$$

Diagram (1) shows that the second norm error of parameter estimation is reached to zero in 6 samples that illustrates the high speed of convergence (high efficiency) for estimator. Now it is possible to obtain the physical parameters from factors by simple mathematical operations and deliver them to the controller for gaining best input for control system. In this context, the results of parameter estimation by common RLS estimator (Figure 2) shows the slow convergence speed comparing to active identification method with the same samples. Table (2) is a numerical comparison between actual and estimated parameters by the two mentioned methods which shows high accuracy of the proposed method.



**Figure 1. Second norm of parameters estimation error in Active Identification**

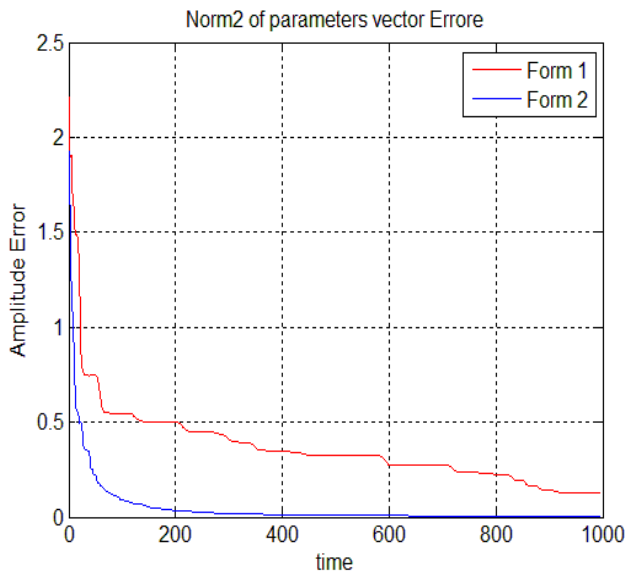


Figure 1. Second norm of parameters estimation error in RLS Estimation

Table 2. Comparison between the convergence of Active and RLS algorithms with the same condition

	R	L <sub>q</sub>	L <sub>d</sub>	λ <sub>f</sub>	j	p	Sample time
Real	2.875	9	7	0.175	8	4	—
Active	2.875	9	7	0.175	8	4	6
RLS	1.9549	15.2866	0.9583	0.0098	-30.61	-67.45	1000

To evaluate the estimated parameters, PRBS signal is applied in parallel to the actual model field voltage and simulated model. Figure (3) that shows the error between these two models, illustrates the accordance of simulated and actual outputs.

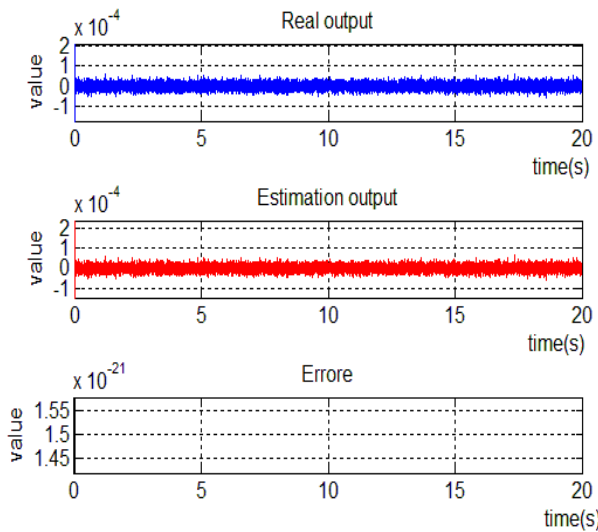


Fig. 3. shows output of real condition and estimated model and their difference. As shown, estimated and real output

One of the widely used criteria to show the error of identification is the normalized residue criterion according to equation (18) [28-29]. Here, this criterion is calculated and is given in Table 3. It is observed that the proposed method has higher superiority to the other methods.

$$J_{dB} = 10 \log \left( \frac{\sum_1^N (y(t) - \hat{y}(t))^2}{\sum_1^N y(t)^2} \right) \quad (18)$$

Table 3. Investigation of normalized residue in two methode.

	The normalized Residual
RLS Methode	-10.8923(dB)
Active Methode	-189.2896(dB)

### 5. CONCLUSION

In this paper, online active identification was proposed for parameter estimation of PMSM. To do this, non-linear model of PMSM was changed into linear regression form without any simplification or linearization, and then parameter estimation was performed in a certain time range. To show the superiority of the estimator, some indices are investigated such as speed of convergence, estimation accuracy and selecting the initial estimation of parameters by the explained criteria. It is understood by the simulation results that active identification method can be an appropriate online estimator for any system where state space model of the system is rewritten to linear regression form.

### REFERENCES

- [1] Yanhui Xu , Vollmer U , Ebrahimi A, Parspour N .Online Estimation of the Stator Resistances of a PMSM with Consideration of Magnetic Saturation. Electrical and Power Engineering Conference and Exposition on (EPE) 2012, 360-365
- [2] Kan Liu, Zhang Q, Chen J.T, Zhu Z.Q., Zhang. J.Online Multiparameter Estimation of Nonsalient-Pole PM Synchronous Machines With Temperature Variation Tracking. IEEE Transactions on industrial electronics 2011; 58(5):1776-1788
- [3] O. Aydogmus ,S. Sünter .Implementation of EKF based sensorless drive system using vector controlled PMSM fed by a matrix converter. Electrical Power and Energy Systems2012; 43(1):736–743
- [4] E.G. Shehata .Speed sensorless torque control of an IPMSM drive with online stator resistance estimation using reduced order EKF. Electrical Power and Energy Systems 2013;47(1):378–386
- [5] Pillay P, Krishnan R.Modeling of Permanent Magnet Motor Drive.IEEE Transactions on industrial electronics, 1988 ;35 (4):537-541
- [6] Nihat Ozturk, Emre Celik .Speed control of permanent magnet synchronous motors using fuzzy controller based on genetic algorithms. Electrical Power and Energy Systems2012; 43 (1): 889–898
- [7] Mehmet AKAR, Sezai TAS,KIN, Serhat S,EKER, Ilyas C,ANKAYA . Detection of static eccentricity for permanent magnet synchronous motors using the coherence analysis. Turk J Elec Eng & Comp Sci2010;18:963-974
- [8] Liu L. , Cartes D.A .Synchronisation based adaptive parameter identification for permanent magnet

- synchronous motors. IET Control Theory , 2007 ; 1(4):1015-1022
- [9] Aymen F, N Martin, Sbita L, Novak J. Online PMSM parameters estimation for 32000rpm. Engineering & Information Technology 2013; 3:148-152
- [10] Chih-Hong Lin, Chih-Peng Lin .The hybrid RFNN control for a PMSM drive electric scooter using rotor flux estimator. Electrical Power and Energy Systems 2012;51:889–898
- [11] Junli G, Yingfan Zh. Reasearch on Parameter Identification and PI Selftuning of PMSM. Information Science and Engineering (ICISE), 2nd International Conference on 2010; 5251-5254
- [12] Kan Liu , Zhu Z.Q .Online Estimation of the Rotor Flux Linkage and Voltage-Source Inverter Nonlinearity in Permanent Magnet Synchronous Machine Drive. Transactions on power electronics, 2014; 29(1):418-427
- [13] Yuchao Shi, Kai Sun, Lipei Huang, and Yongdong Li. Online Identification of Permanent Magnet Flux Based on Extended Kalman Filter for IPMSM Drive With Position Sensorless Control. Transactions on industrial electronics, 2012; 59(11):4169-4178
- [14] Nahid Mobarakeh B, Meibody-Tabar F, Sargos F M. .On-line Identification of PMSM Electrical Parameters Based on Decoupling Control.; 1:266-273
- [15] Boileau, T.; Leboeuf N, Nahid Mobarakeh B , Meibody-Tabar F. Online Identification of PMSM Parameters: Parameter Identifiability and Estimator Comparative Study. Transactions on industry applications 2011; 47(4):1944-1957
- [16] Boileau T. ; Nahid-Mobarakeh B. ; Meibody-Tabar F. .On-line Identification of PMSM Parameters: Model-Reference vs EKF. Industry Applications Society Annual Meeting 2008; 1-8
- [17] Kan Liu, Qiao Zhang, Jintao Chen, Z. Q. Zhu and Jing Zhang .Online Multiparameter Estimation of Nonsalient-Pole PM Synchronous Machines With Temperature Variation Tracking. Transactions on industrial electronics 2011 ; 58(5): 1776-1788
- [18] Aymen F, N Martin, Sbita L, Novak J. Online PMSM parameters estimation for 32000rpm. Engineering & Information Technology 2013; 3:148-152
- [19] Kan Liu ; Zhu, Z.Q ; Stone D.A. .Parameter Estimation for Condition Monitoring of PMSM Stator Winding and Rotor Permanent Magnets. Transactions on industrial electronics 2013; 60(12): 5902-5913
- [20] Agahi H ; Karrari M, Rosehart W., Malik O.P. Application of Active Identification Method to Synchronous Generator Parameter Estimation. IEEE PES General Meeting, Montreal, Canada June 2006, 18-22
- [21] Agahi, H ; Karrari, M ; Mahmoodzadeh, A . Combination of orthogonalized projection algorithm and recursive least square method for estimation objectives. XVI International Conference on Systems Science (SYSTEMS SCIENCE XVI), September 4-6, 2007
- [22] Agahi, H. Active Identification for Nonlinear Multivariable System Identification and Its application for Synchronous Generator Identification. PhD thesis, Amirkabir University of Technology Tehran, Iran, May 2007
- [23] Ghanbari M, Yousefi I, Mossadegh V. online parameter estimation of permanent magnet synchronous motor using orthogonal projection algorithm. indian journal scientific research ; 2(1):2014 32-36
- [24] Chiasson J. MODELING AND CONTROL OF ELECTRIC MACHINES HIGH-PERFORMANCE. IEEE Power Engineering Mohamed E. El-Hawary, Series Editor 2005
- [25] A K Parvathy, R. Devanathan, V. Kamaraj .Application of quadratic linearization to control of Permanent Magnet synchronous motor. Power System Technology and IEEE Power India Conference, 2008:158-163
- [26] Hamida, M.A. ; De Leon, J. ; Glumineau, A. ; Boisliveau, R. .An Adaptive Interconnected Observer for Sensorless Control of PM Synchronous Motors With Online Parameter Identification Transactions on industrial electronics 2013; 60(2):739-748
- [27] R. Krishnan. Permanent Magnet Synchronous and Brushless DC Motor Drives” Electrical and Computer Engineering Department Virginia Tech Blacksburg, Virginia, U.S.A., 2010 by Taylor and Francis Group, LLC
- [28] Ghanbari M. , Haeri M .Parametric identification of fractional-order systems using a fractional Legendre basis. Proc. IMechE, Part I: J. Systems and Control Engineering 2010;224(13):261-274
- [29] Ghanbari M, Haeri M. Order and pole locator estimation in fractional ordersystems using Bode diagram. Signal Processing 2011;91(2):191-202
- [30] Jiaxiang Zhao and Ioannis Kanellakopoulos .Active Identification for Discrete-Time Nonlinear Control— Part I: Output-Feedback Systems Transactions on automatic control 2002; 47(2):210-224