

ADAPTIVE LAG SYNCHRONIZATION OF A MODIFIED RUCKLIDGE CHAOTIC SYSTEM WITH UNKNOWN PARAMETERS AND ITS LABVIEW IMPLEMENTATION

¹Karthikeyan Rajagopal and ²Sundarapandian Vaidyanathan

¹ Department of Electronics Engineering, Defense Engineering College, DebreZeit, Ethiopia
rkarthikeyan@gmail.com

² Research and Development Centre, Vel Tech University, Avadi, Chennai-600 062, India
sundarvtu@gmail.com

ABSTRACT—Chaos theory has wide applications in several branches of science and engineering. The discovery of novel chaotic systems in various applications, their qualitative properties and the control of such systems are active research areas. This paper announces a novel chaotic system obtained by modifying the equations of the Rucklidge chaotic system (1992) for nonlinear double convection. The Lyapunov exponents of the modified Rucklidge chaotic system are obtained as $L_1 = 0.4283$, $L_2 = 0$ and $L_3 = -3.4301$. Also, the Lyapunov dimension of the modified Rucklidge chaotic system is derived as $D_L = 2.1249$. Next, an adaptive feedback controller is defined for the lag synchronization of the identical modified Rucklidge chaotic systems with unknown parameters. Finally, a circuit design of the modified Rucklidge chaotic system and its adaptive lag synchronization are implemented in LabVIEW to validate the results for the theoretical chaotic model.

Keywords— chaos; chaotic systems; Rucklidge system; delay systems; lag synchronization; circuit design; LabVIEW.

I. INTRODUCTION

A chaotic system is usually characterized by having a dense collection of points with periodic orbits, being sensitive to initial conditions of the system (“butterfly effect”) and also being topologically transitive. A chaotic system is also characterized by the existence of a positive Lyapunov exponent.

The first chaotic system was derived by Lorenz [1], when he was studying convection patterns in the weather model. Numerous 3-D chaotic systems have been found in recent decades such as Rössler system [2], ACT system [3], Rucklidge system [4], Chen system [5], Lü system [6], Chen-Lee system [7], Wang system [8], Zhang-Tang system [9], Sundarapandian-Pehlivan system [10], Pehlivan system [11], Vaidyanathan systems [12-28], Thanh system [29-30], etc.

Chaos modelling have applications in many areas such as chemical reactors [31-40], Brusselators [41-43], Dynamo systems [44-48], Tokamak systems [49-50], biology models [51-60], neurology [61-70], ecology models [71-77], memristive devices [78-80], economics [81-82], etc.

Recently, many methods have been developed in the control literature for synchronizing a pair of chaotic systems such as active control [83-100], adaptive control [101-120], backstepping control [121-130], sliding control [131-140], etc.

Due to the presence of signal propagation delays, we cannot always assume that the states in the response system should synchronize with the driving signals at exactly the same time. Thus, in designing a controller for synchronizing chaotic systems, the propagation delays should be taken into consideration. In such a case, the response state $y(t)$ is expected to synchronize with the driving signal with certain transmission lag τ . In other words, the synchronization goal aims to drive the lag synchronization error $e(t) = y(t) - x(t - \tau)$ to zero asymptotically as $t \rightarrow \infty$.

Lag synchronization is investigated with many approaches such as intermittent control [141], adaptive control [142], sliding mode control [143], fuzzy logic control [144], etc.

In fluid mechanics modelling, cases of two-dimensional convection in a horizontal layer of Boussinesq fluid with lateral constraints were studied by Rucklidge [4]. When the convection takes place in a fluid layer rotating uniformly about a vertical axis and in the limit of tall thin rolls, convection in an imposed vertical magnetic field and convection in a rotating fluid layer are both modeled by the Rucklidge system of ordinary differential equations, which produces chaotic solutions like the Lorenz system [1].

In this research work, we derive a novel chaotic system by modifying the equations of the Rucklidge chaotic system [4]. We discuss the qualitative properties of the modified Rucklidge chaotic system such as dissipativity, stability of the equilibrium points, Lyapunov exponents and Lyapunov dimension. Next, we derive new results for the lag synchronization of the identical modified Rucklidge chaotic systems via adaptive control method. Finally, we present details of the circuit simulation and LabVIEW implementation of the modified Rucklidge chaotic system and adaptive lag synchronization of the modified Rucklidge chaotic systems.

II. A MODIFIED RUCKLIDGE CHAOTIC SYSTEM

The Rucklidge chaotic system [4] for nonlinear double convection is described by

$$\begin{aligned}\dot{x}_1 &= -ax_1 + bx_2 - x_2x_3 \\ \dot{x}_2 &= x_1 \\ \dot{x}_3 &= -x_3 + x_2^2\end{aligned}\quad (1)$$

where x_1, x_2, x_3 are the states and a, b are constant, positive, parameters.

The Rucklidge system (1) is *chaotic* when the parameter values are taken as

$$a = 2, \quad b = 6.7 \quad (2)$$

The Lyapunov exponents of the Rucklidge system (1) are obtained numerically as

$$L_1 = 0.1877, \quad L_2 = 0, \quad L_3 = -3.1893 \quad (3)$$

Also, the Lyapunov dimension of the Rucklidge chaotic system (1) is derived as

$$D_L = 2 + \frac{L_1 + L_2}{|L_3|} = 2.0589 \tag{4}$$

In this research work, we derive a novel chaotic system by modifying the equations of the Rucklidge chaotic system (1) and we obtain the novel system

$$\begin{aligned} \dot{x}_1 &= -ax_1 + bx_2 - x_2x_3 \\ \dot{x}_2 &= x_1 \\ \dot{x}_3 &= -x_3 + x_2^4 \end{aligned} \tag{5}$$

In this work, we show that the modified Rucklidge system (5) is chaotic when the parameter values are taken as

$$a = 2, \quad b = 10 \tag{6}$$

For numerical simulations, we take the initial conditions of the modified Rucklidge system (5) as

$$x_1(0) = 1.2, \quad x_2(0) = 0.8, \quad x_3(0) = 1.4 \tag{7}$$

The basic qualitative properties of the modified Rucklidge chaotic system (5) are described in Section III.

The Lyapunov exponents of the modified Rucklidge chaotic system (5) are obtained as

$$L_1 = 0.4283, \quad L_2 = 0, \quad L_3 = -3.4301 \tag{8}$$

Also, the Lyapunov dimension of the modified Rucklidge chaotic system (5) is derived as

$$D_L = 2 + \frac{L_1 + L_2}{|L_3|} = 2.1249 \tag{9}$$

It is noted that the Maximal Lyapunov Exponent (MLE) of the modified Rucklidge chaotic system (5) is greater than that of the Rucklidge chaotic system (1). It is also noted that the Lyapunov dimension of the modified Rucklidge chaotic system (5) is greater than that of the Rucklidge chaotic system (1). This shows that the modified Rucklidge chaotic system (5) has more chaotic behavior than the Rucklidge chaotic system (1).

Fig. 1 shows the strange chaotic attractor of the modified Rucklidge chaotic system (5).

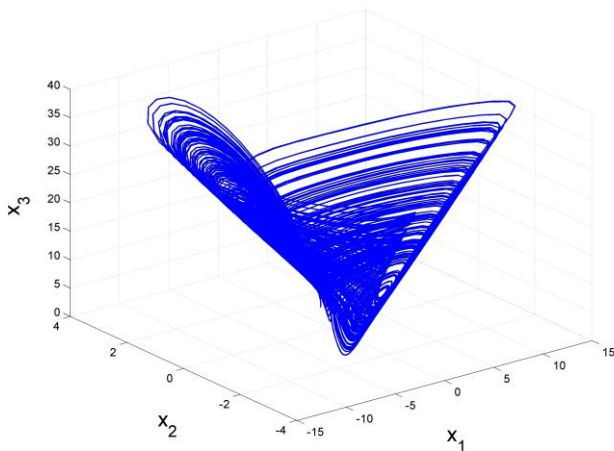


Fig. 1 Strange attractor of the modified Rucklidge chaotic system

The modified Rucklidge chaotic system with delay is given by the 3-D dynamics

$$\begin{aligned} \dot{x}_1(t-\tau) &= -ax_1(t-\tau) + bx_2(t-\tau) - x_2(t-\tau)x_3(t-\tau) \\ \dot{x}_2(t-\tau) &= x_1(t-\tau) \\ \dot{x}_3(t-\tau) &= -x_3(t-\tau) + x_2^4(t-\tau) \end{aligned} \tag{10}$$

where $\tau > 0$ is the time-delay and a, b are constant, positive parameters.

III. ANALYSIS OF THE MODIFIED RUCKLIDGE CHAOTIC SYSTEM

A. Dissipativity

In vector notation, the modified Rucklidge system (5) can be expressed as

$$\dot{x} = f(x) = \begin{bmatrix} f_1(x) \\ f_2(x) \\ f_3(x) \end{bmatrix}. \tag{11}$$

The divergence on the vector field f on R^3 is given by

$$\nabla \cdot f = \frac{\partial f_1(x)}{\partial x_1} + \frac{\partial f_2(x)}{\partial x_2} + \frac{\partial f_3(x)}{\partial x_3}. \tag{12}$$

Let Ω be any region in R^3 with a smooth boundary. Let $\Omega(t) = \Phi_t(\Omega)$, where Φ_t is the flow of f . Let $V(t)$ denote the volume of $\Omega(t)$.

By Liouville's theorem, we have

$$\dot{V}(t) = \int_{\Omega(t)} (\nabla \cdot f) dx_1 dx_2 dx_3 \tag{13}$$

The divergence of the flow of the system (5) is found as

$$\nabla \cdot f = \frac{\partial f_1}{\partial x_1} + \frac{\partial f_2}{\partial x_2} + \frac{\partial f_3}{\partial x_3} = -(a+1) = -\mu \tag{14}$$

where $\mu = a+1 = 3 > 0$.

Substituting the value of $\nabla \cdot f$ in (13), we get

$$\dot{V}(t) = \int_{\Omega(t)} (-\mu) dx_1 dx_2 dx_3 = -\mu V(t) \tag{15}$$

Integrating the linear differential equation (15), we get

$$V(t) = \exp(-\mu t)V(0) \tag{16}$$

Since $\mu > 0$, it follows from Eq. (16) that $V(t) \rightarrow 0$ exponentially as $t \rightarrow \infty$. Thus, the modified Rucklidge system (5) is dissipative. Thus, the system limit sets are ultimately confined into a specific limit set of zero volume, and the asymptotic motion of the system (5) settles onto a strange attractor of the system.

B. Symmetry

The system (5) is invariant under the coordinates transformation

$$(x_1, x_2, x_3) \mapsto (-x_1, -x_2, x_3) \tag{17}$$

The transformation (17) persists for all values of the system parameters. Thus, the system (5) has rotation symmetry about

the x_3 – axis and any non-trivial trajectory of the system (5) must have a twin trajectory.

C. Invariance

It is easy to see that the x_3 – axis is invariant for the flow of the system (5). Also, the invariant motion of the flow of the system on the x_3 – axis is governed by the scalar differential equation

$$\dot{x}_3 = -x_3 \tag{18}$$

which is globally exponentially stable.

D. Lyapunov Exponents and Lyapunov Dimension

We take the parameter values of the modified Rucklidge system (5) as in the chaotic case, i.e.

$$a = 2, \quad b = 10 \tag{19}$$

We take the initial state as

$$x_1(0) = 1.2, \quad x_2(0) = 0.8, \quad x_3(0) = 1.4 \tag{20}$$

The Lyapunov exponents of the modified Rucklidge system (5) are numerically obtained using MATLAB as

$$L_1 = 0.4283, \quad L_2 = 0, \quad L_3 = -3.4307 \tag{21}$$

Eq. (29) shows that the modified Rucklidge system (5) is a chaotic system since it has a positive Lyapunov exponent, L_1 .

Since $L_1 + L_2 + L_3 = -3.0018 < 0$, it is immediate that the modified Rucklidge chaotic system (5) is dissipative.

The Lyapunov dimension of the modified Rucklidge chaotic system (5) is determined as

$$D_L = 2 + \frac{L_1 + L_2}{|L_3|} = 2.1249, \tag{22}$$

which is fractional.

IV. ADAPTIVE LAG SYNCHRONIZATION OF MODIFIED RUCKLIDGE CHAOTIC SYSTEMS

For the master system defined by the modified Rucklidge chaotic system (10) with unknown parameters a and b , the slave system can be described as

$$\begin{aligned} \dot{y}_1 &= -ay_1 + by_2 - y_2y_3 + u_1 \\ \dot{y}_2 &= y_1 + u_2 \\ \dot{y}_3 &= -y_3 + y_2^4 + u_3 \end{aligned} \tag{23}$$

where u_1, u_2, u_3 are nonlinear controllers to be designed using estimates $\hat{a}(t), \hat{b}(t)$ of the unknown system parameters so that the systems (10) and (23) can be synchronized.

The lag synchronization error is defined as

$$\begin{aligned} e_1(t) &= y_1(t) - x_1(t - \tau) \\ e_2(t) &= y_2(t) - x_2(t - \tau) \\ e_3(t) &= y_3(t) - x_3(t - \tau) \end{aligned} \tag{24}$$

where $\tau > 0$ is a constant representing time delay or lag. Then the lag synchronization error dynamics can be easily obtained as

$$\begin{aligned} \dot{e}_1 &= -ae_1 + be_2 - y_2(t)y_3(t) \\ &\quad + x_2(t - \tau)x_3(t - \tau) + u_1 \\ \dot{e}_2 &= e_1 + u_2 \\ \dot{e}_3 &= -e_3 + y_2^4(t) - x_2^4(t - \tau) + u_3 \end{aligned} \tag{25}$$

We consider an adaptive feedback controller defined by

$$\begin{aligned} u_1 &= \hat{a}(t)e_1 - \hat{b}(t)e_2 + y_2(t)y_3(t) \\ &\quad - x_2(t - \tau)x_3(t - \tau) - k_1e_1 \\ u_2 &= -e_1 - k_2e_2 \\ u_3 &= e_3 - y_2^4(t) + x_2^4(t - \tau) - k_3e_3 \end{aligned} \tag{26}$$

where $\hat{a}(t), \hat{b}(t)$ are estimates of the unknown parameters a, b , respectively, and k_1, k_2, k_3 are positive gain constants.

Substituting (26) into (25), we obtain the closed-loop error dynamics as

$$\begin{aligned} \dot{e}_1 &= -[a - \hat{a}(t)]e_1 + [b - \hat{b}(t)]e_2 - k_1e_1(t) \\ \dot{e}_2 &= -k_2e_2(t) \\ \dot{e}_3 &= -k_3e_3(t) \end{aligned} \tag{27}$$

We define the parameter estimation errors as

$$\begin{aligned} e_a(t) &= a - \hat{a}(t) \\ e_b(t) &= b - \hat{b}(t) \end{aligned} \tag{28}$$

Substituting (28) into (27), we get the error dynamics as

$$\begin{aligned} \dot{e}_1 &= -e_a e_1 + e_b e_2 - k_1 e_1(t) \\ \dot{e}_2 &= -k_2 e_2(t) \\ \dot{e}_3 &= -k_3 e_3(t) \end{aligned} \tag{29}$$

Differentiating (28), we obtain

$$\begin{aligned} \dot{e}_a &= -\dot{\hat{a}}(t) \\ \dot{e}_b &= -\dot{\hat{b}}(t) \end{aligned} \tag{30}$$

Next, we consider the Lyapunov function defined by

$$V = \frac{1}{2} (e_1^2 + e_2^2 + e_3^2 + e_a^2 + e_b^2), \tag{31}$$

which is positive definite on R^5 .

Differentiating V along the trajectories of (29) and (30), we obtain

$$\begin{aligned} \dot{V} &= -k_1 e_1^2 - k_2 e_2^2 - k_3 e_3^2 + e_a [-e_1^2 - \dot{\hat{a}}] \\ &\quad + e_b [e_1 e_2 - \dot{\hat{b}}] \end{aligned} \tag{32}$$

In view of (32), we take the parameter update law as

$$\begin{aligned} \dot{\hat{a}} &= -e_1^2 \\ \dot{\hat{b}} &= e_1 e_2 \end{aligned} \tag{33}$$

Next, we state the main result of this section.

Theorem 1. The time-delayed modified Rucklidge chaotic system (10) and the modified Rucklidge chaotic system (23) with unknown system parameters are globally and exponentially synchronized by the adaptive feedback control law (26) and the parameter update law (33), where k_1, k_2, k_3 are positive gain constants.

Proof. Substituting (33) into (32), we obtain the time-derivative of the quadratic Lyapunov function V as

$$\dot{V} = -k_1 e_1^2 - k_2 e_2^2 - k_3 e_3^2 \tag{34}$$

which is a negative semi-definite function on R^5 . Thus, using Barbalat's lemma [145], we conclude that $e(t) \rightarrow 0$ as $t \rightarrow \infty$ for all initial conditions $e(0) \in R^3$. This completes the proof. ■

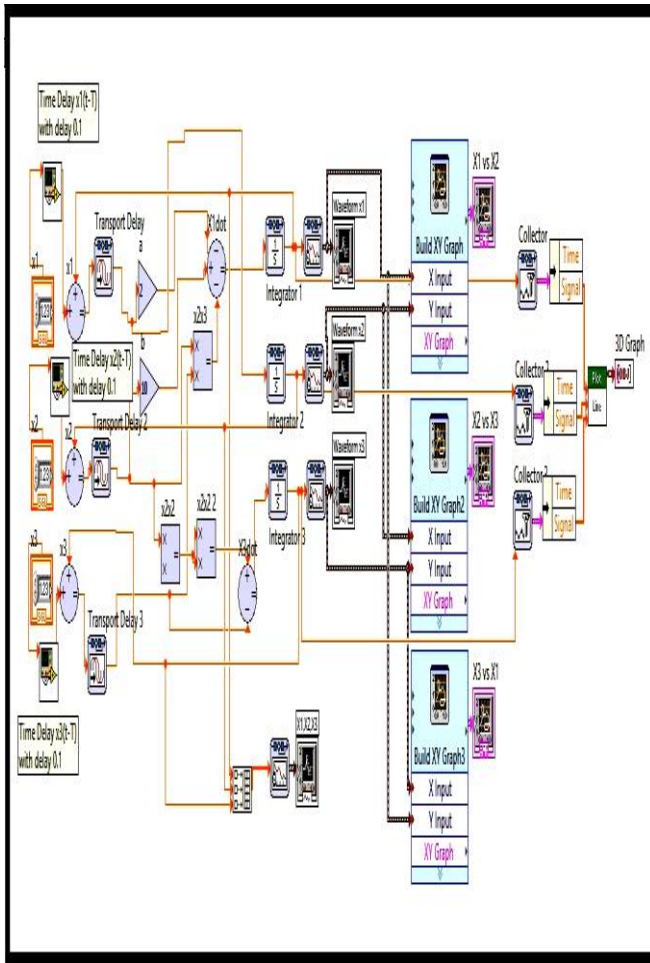


Fig. 2 LabVIEW implementation of the time-delayed modified Rucklidge chaotic system

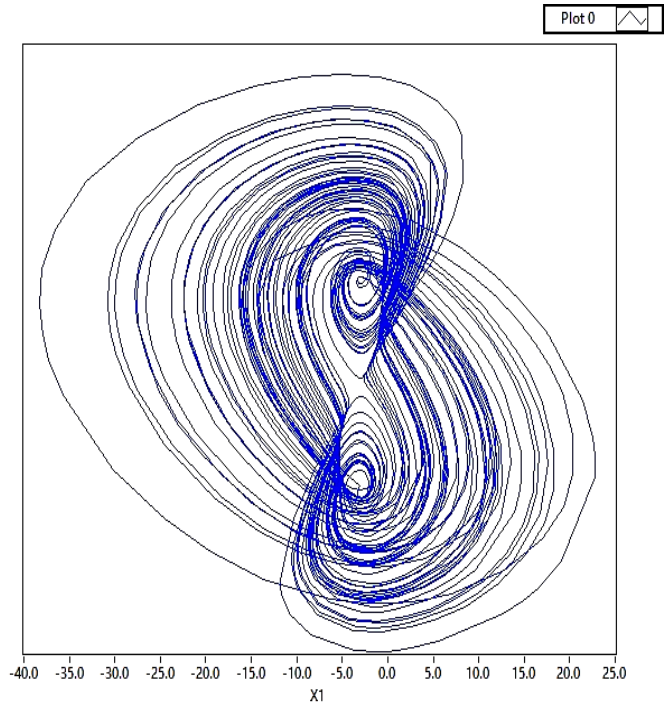


Fig. 3 (x_1, x_2) -phase portrait of the time-delayed modified Rucklidge chaotic system

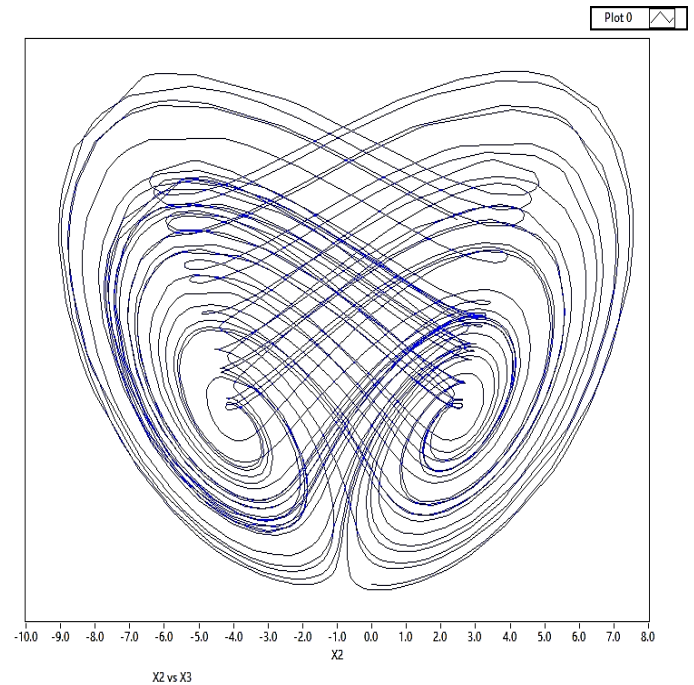


Fig. 4 (x_2, x_3) -phase portrait of the time-delayed modified Rucklidge chaotic system

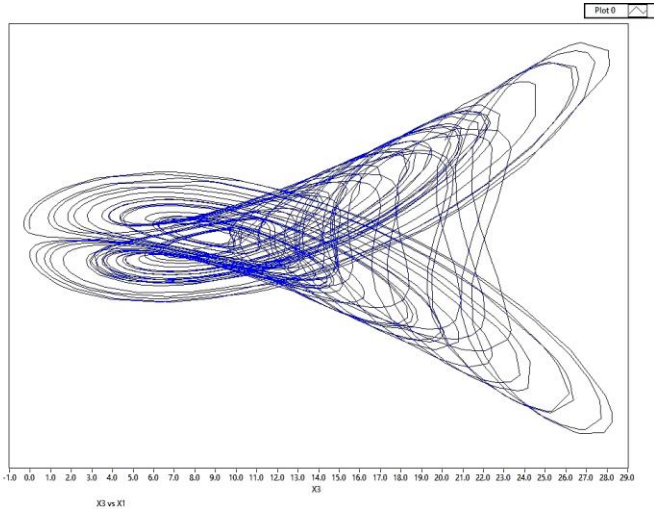


Fig. 5 (x_3, x_1) -phase portrait of the time-delayed modified Rucklidge chaotic system

V. LABVIEW IMPLEMENTATION OF THE MODIFIED RUCKLIDGE CHAOTIC SYSTEM

Fig. 2 shows the implementation of the modified Rucklidge chaotic system (10) in LabVIEW using the Control Design and Simulation Loop.

For numerical simulations, we take

$$\tau = 0.1, a = 2, b = 10 \tag{35}$$

and initial state as

$$x_1(0) = 1.2, x_2(0) = 0.8, x_3(0) = 1.4. \tag{36}$$

Figures 3-5 show the 2-D phase portraits of the modified Rucklidge chaotic system (10).

VI. LABVIEW IMPLEMENTATION OF THE ADAPTIVE LAG SYNCHRONIZATION OF THE MODIFIED RUCKLIDGE SYSTEMS

In this section, the adaptive control method for the lag synchronization of the modified Rucklidge chaotic systems discussed in Section III is implemented using LabVIEW.

Fig. 6 shows the design of slave subsystem (23) using LabVIEW. Fig. 7 shows the design in LabVIEW for the adaptive controller u defined by Eq. (26).

For numerical simulations, the initial values of the master system (10) are taken as

$$x_1(0) = 1.4, x_2(0) = 1.2, x_3(0) = 0.8 \tag{37}$$

The initial values of the slave system (23) are taken as

$$y_1(0) = 0.4, y_2(0) = 1.7, y_3(0) = 0.5 \tag{38}$$

The initial values of the parameter estimates are taken as

$$\hat{a}(0) = 0.8, \hat{b}(0) = 6.3 \tag{39}$$

The time-delay is taken as $\tau = 0.1$.

Fig. 8 shows the time history of the lag synchronization errors.

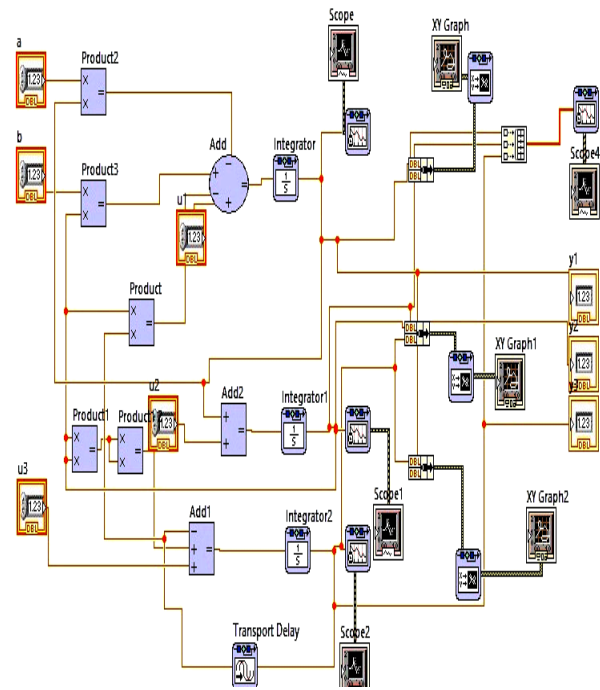


Fig. 6 LabVIEW implementation of the slave system

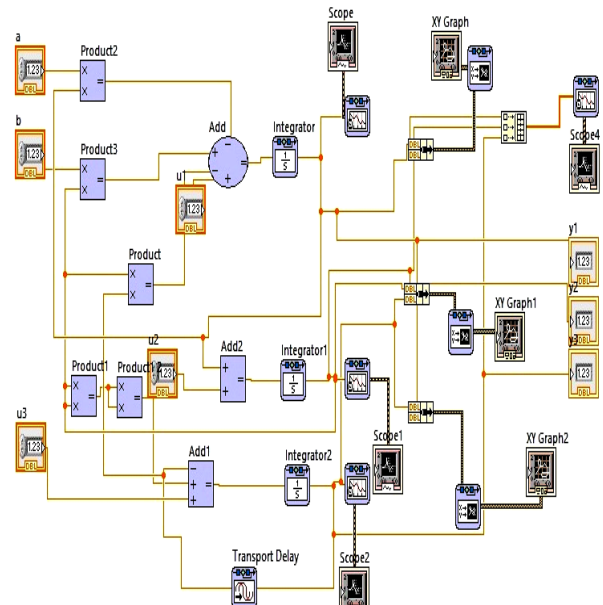


Fig. 7 LabVIEW implementation of the adaptive controller for lag synchronization

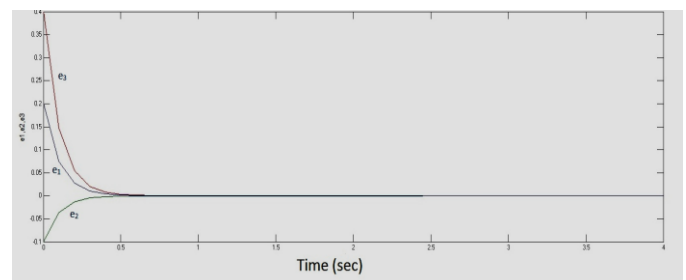


Fig. 8 Time-history of the lag synchronization errors

VII. CONCLUSIONS

In this paper, we have discovered a novel chaotic system, which has been obtained by modifying the equations of the Rucklidge chaotic system (1992) for nonlinear double convection. The qualitative properties of the modified Rucklidge chaotic system have been derived. It is also noted that the modified Rucklidge chaotic system is dissipative. This research work also derived new results for the adaptive lag synchronization of identical modified Rucklidge chaotic systems. To validate the results for the theoretical model, we presented LabVIEW implementation of the modified Rucklidge chaotic system with delay and adaptive controller design for the lag synchronization of the modified Rucklidge chaotic systems.

REFERENCES

- [1] E.N. Lorenz, "Deterministic nonperiodic flow," *Journal of the Atmospheric Sciences*, vol. 20, pp. 130-141, 1963.
- [2] O.E. Rössler, "An equation for continuous chaos," *Physics Letters A*, vol. 57, no. 5, pp. 397-398, 1976.
- [3] A. Arneodo, P. Couillet and C. Tresser, "Possible new strange attractors with spiral structure," *Communications in Mathematical Physics*, vol. 79, pp. 573-579, 1981.
- [4] A.M. Rucklidge, "Chaos in models of double convection," *Journal of Fluid Mechanics*, vol. 237, pp. 209-229, 1992.
- [5] G. Chen and T. Ueta, "Yet another chaotic attractor," *International Journal of Bifurcation and Chaos*, vol. 9, pp. 1465-1466, 1999.
- [6] J. Lü and G. Chen, "A new chaotic attractor coined," *International Journal of Bifurcation and Chaos*, vol. 12, pp. 659-661, 2002.
- [7] H.K. Chen and C.I. Lee, "Anti-control of chaos in rigid body motion," *Chaos, Solitons and Fractals*, vol. 21, pp. 957-965, 2004.
- [8] J. Wang, Z. Chen and Z. Yuan, "Existence of a new three-dimensional chaotic attractor," *Chaos, Solitons and Fractals*, vol. 42, pp. 3053-3057, 2009.
- [9] J. Zhang and W. Tang, "Analysis and control for a new chaotic system via piecewise linear feedback," *Chaos, Solitons and Fractals*, vol. 42, pp. 2181-2190, 2009.
- [10] V. Sundarapandian and I. Pehlivan, "Analysis, control, synchronization and circuit design of a novel chaotic system," *Mathematical and Computer Modelling*, vol. 55, pp. 1904-1915, 2012.
- [11] I. Pehlivan, I.M. Moroz and S. Vaidyanathan, "Analysis, synchronization and circuit design of a novel butterfly attractor," *Journal of Sound and Vibration*, vol. 333, no. 20, pp. 5077-5096, 2014.
- [12] S. Vaidyanathan, "A new six-term 3-D chaotic system with an exponential nonlinearity," *Far East Journal of Mathematical Sciences*, vol. 79, no. 1, pp. 135-143, 2013.
- [13] V. Sundarapandian, "Analysis and anti-synchronization of a novel chaotic system via active and adaptive controllers," *Journal of Engineering Science and Technology Review*, vol. 6, no. 4, pp. 45-52, 2013.
- [14] S. Vaidyanathan, "A new eight-term 3-D polynomial chaotic system with three quadratic nonlinearities," *Far East Journal of Mathematical Sciences*, vol. 84, no. 2, pp. 219-226, 2014.
- [15] S. Vaidyanathan, "Analysis, control and synchronisation of a six-term novel chaotic system with three quadratic nonlinearities," *International Journal of Modelling, Identification and Control*, vol. 22, no. 1, pp. 41-53, 2014.
- [16] S. Vaidyanathan, C. Volos, V.-T. Pham, K. Madhavan and B.A. Idowu, "Adaptive backstepping control, synchronization and circuit simulation of a 3-D novel jerk chaotic system with two hyperbolic sinusoidal nonlinearities," *Archives of Control Sciences*, vol. 24, no. 3, pp. 375-403, 2014.
- [17] S. Vaidyanathan, "Analysis and adaptive synchronization of eight-term 3-D polynomial chaotic systems with three quadratic nonlinearities," *European Physical Journal: Special Topics*, vol. 223, no. 8, pp. 1519-1529, 2014.
- [18] S. Vaidyanathan, "Generalized projective synchronisation of novel 3-D chaotic systems with an exponential non-linearity via active and adaptive control," *International Journal of Modelling, Identification and Control*, vol. 22, no. 3, pp. 207-217, 2014.
- [19] S. Vaidyanathan, "Qualitative analysis, adaptive control and synchronization of a seven-term novel 3-D chaotic system with a quartic nonlinearity," *International Journal of Control Theory and Applications*, vol. 7, no. 1, pp. 1-20, 2014.
- [20] S. Vaidyanathan, C.K. Volos and V.-T. Pham, "Analysis, adaptive control and adaptive synchronization of a nine-term novel 3-D chaotic system with four quadratic nonlinearities and its circuit simulation," *Journal of Engineering Science and Technology Review*, vol. 8, no. 2, pp. 181-191, 2015.
- [21] S. Vaidyanathan, K. Rajagopal, C.K. Volos, I.M. Kyprianidis and I.N. Stouboulos, "Analysis, adaptive control and synchronization of a seven-term novel 3-D chaotic system with three quadratic nonlinearities and its digital implementation in LabVIEW," *Journal of Engineering Science and Technology Review*, vol. 8, no. 2, pp. 130-141, 2015.
- [22] S. Vaidyanathan, "Analysis, properties and control of an eight-term 3-D chaotic system with an exponential nonlinearity," *International Journal of Modelling, Identification and Control*, vol. 23, no. 2, pp. 164-172, 2015.
- [23] S. Vaidyanathan and A.T. Azar, "Analysis, control and synchronization of a nine-term 3-D novel chaotic system," *Studies in Computational Intelligence*, vol. 581, pp. 19-38, 2015.
- [24] S. Sampath, S. Vaidyanathan, C.K. Volos and V.-T. Pham, "An eight-term novel four-scroll chaotic system with cubic nonlinearity and its circuit simulation," *Journal of Engineering Science and Technology Review*, vol. 8, no. 2, pp. 1-6, 2015.
- [25] S. Vaidyanathan, C.K. Volos, I.M. Kyprianidis, I.N. Stouboulos and

- V.-T. Pham, "Analysis, adaptive control and anti-synchronization of a six-term novel jerk chaotic system with two exponential nonlinearities and its circuit simulation," *Journal of Engineering Science and Technology Review*, vol. 8, no. 2, pp. 24-36, 2015.
- [26] S. Vaidyanathan, C.K. Volos and V.-T. Pham, "Global chaos control of a novel nine-term chaotic system via sliding mode control," *Studies in Computational Intelligence*, vol. 576, pp. 571-590, 2015.
- [27] S. Vaidyanathan and C. Volos, "Analysis and adaptive control of a novel 3-D conservative no-equilibrium chaotic system," *Archives of Control Sciences*, vol. 25, no. 3, pp. 333-353, 2015.
- [28] S. Vaidyanathan, "A 3-D novel highly chaotic system with four quadratic nonlinearities, its adaptive control and anti-synchronization with unknown parameters," *Journal of Engineering Science and Technology Review*, vol. 8, no. 2, pp. 106-115, 2015.
- [29] V.T. Pham, S. Vaidyanathan, C.K. Volos and S. Jafari, "Hidden attractors in a chaotic system with an exponential nonlinear term," *European Physical Journal: Special Topics*, vol. 224, no. 8, pp. 1507-1517, 2015.
- [30] V.-T. Pham, C.K. Volos and S. Vaidyanathan, "Multi-scroll chaotic oscillator based on a first-order delay differential equation," *Studies in Computational Intelligence*, vol. 581, pp. 59-72, 2015.
- [31] Y. Huang and X.S. Yang, "Chaoticity of some chemical attractors: a computer assisted proof," *Journal of Mathematical Chemistry*, vol. 38, pp. 107-117, 2005.
- [32] S. Vaidyanathan, "Adaptive synchronization of novel 3-D chemical chaotic reactor systems," *International Journal of ChemTech Research*, vol. 8, no. 7, pp. 159-171, 2015.
- [33] S. Vaidyanathan, "A novel chemical chaotic reactor system and its adaptive control," *International Journal of ChemTech Research*, vol. 8, no. 7, pp. 146-158, 2015.
- [34] S. Vaidyanathan, "Adaptive synchronization of chemical chaotic reactors," *International Journal of ChemTech Research*, vol. 8, no. 2, pp. 612-621, 2015.
- [35] S. Vaidyanathan, "Adaptive control design for the anti-synchronization of novel 3-D chemical chaotic reactor systems," *International Journal of ChemTech Research*, vol. 8, no. 11, pp. 654-668, 2015.
- [36] S. Vaidyanathan, "Integral sliding mode control design for the global chaos synchronization of identical novel chemical chaotic reactor systems," *International Journal of ChemTech Research*, vol. 8, no. 11, pp. 684-699, 2015.
- [37] S. Vaidyanathan, "A novel chemical chaotic reactor system and its output regulation via integral sliding mode control," *International Journal of ChemTech Research*, vol. 8, no. 11, pp. 669-683, 2015.
- [38] S. Vaidyanathan, "Global chaos synchronization of chemical chaotic reactors via novel sliding mode control method," *International Journal of ChemTech Research*, vol. 8, no. 7, pp. 209-221, 2015.
- [39] S. Vaidyanathan, "Adaptive control of a chemical chaotic reactor," *International Journal of PharmTech Research*, vol. 8, no. 3, pp. 377-382, 2015.
- [40] S. Vaidyanathan, "Anti-synchronization of chemical chaotic reactors via adaptive control method," *International Journal of ChemTech Research*, vol. 8, no. 8, pp. 73-85, 2015.
- [41] S. Vaidyanathan, "Anti-synchronization of Brusselator chemical reaction systems via adaptive control," *International Journal of ChemTech Research*, vol. 8, no. 6, pp. 759-768, 2015.
- [42] S. Vaidyanathan, "Anti-synchronization of Brusselator chemical reaction systems via integral sliding mode control," *International Journal of ChemTech Research*, vol. 8, no. 11, pp. 700-713, 2015.
- [43] S. Vaidyanathan, "Dynamics and control of Brusselator chemical reaction," *International Journal of ChemTech Research*, vol. 8, no. 6, pp. 740-749, 2015.
- [44] S. Vaidyanathan, "Adaptive synchronization of Rikitake two-disk dynamo chaotic systems," *International Journal of ChemTech Research*, vol. 8, no. 8, pp. 100-111, 2015.
- [45] S. Vaidyanathan, "Anti-synchronization of Rikitake two-disk dynamo chaotic systems via adaptive control method," *International Journal of ChemTech Research*, vol. 8, no. 9, pp. 393-405, 2015.
- [46] S. Vaidyanathan, "State regulation of Rikitake two-disk dynamo chaotic system via adaptive control method," *International Journal of ChemTech Research*, vol. 8, no. 9, pp. 374-386, 2015.
- [47] S. Vaidyanathan, "Adaptive control of Rikitake two-disk dynamo chaotic system," *International Journal of ChemTech Research*, vol. 8, no. 8, pp. 121-133, 2015.
- [48] S. Vaidyanathan, "Hybrid chaos synchronization of Rikitake two-disk dynamo chaotic systems via adaptive control method," *International Journal of ChemTech Research*, vol. 8, no. 11, pp. 12-25, 2015.
- [49] S. Vaidyanathan, "Dynamics and control of Tokamak system with symmetric and magnetically confined plasma," *International Journal of ChemTech Research*, vol. 8, no. 6, pp. 795-803, 2015.
- [50] S. Vaidyanathan, "Synchronization of Tokamak systems with symmetrically and magnetically confined plasma via adaptive control," *International Journal of ChemTech Research*, vol. 8, no. 6, pp. 818-827, 2015.
- [51] S. Vaidyanathan, "Anti-synchronization of FitzHugh-Nagumo chaotic neuron models via adaptive control method," *International Journal of PharmTech Research*, vol. 8, no. 7, pp. 71-83, 2015.
- [52] S. Vaidyanathan, "Adaptive control of the FitzHugh-Nagumo chaotic neuron model," *International Journal of PharmTech Research*, vol. 8, no. 6, pp. 117-127, 2015.
- [53] S. Vaidyanathan, "Adaptive synchronization of the identical FitzHugh-Nagumo chaotic neuron models," *International Journal of PharmTech Research*, vol. 8, no. 6, pp. 167-177, 2015.
- [54] S. Vaidyanathan, "Global chaos synchronization of novel coupled Van der Pol conservative chaotic systems via adaptive control method," *International*

- Journal of PharmTech Research, vol. 8, no. 8, pp. 95-111, 2015.
- [55] S. Vaidyanathan, "A novel coupled Van der Pol conservative chaotic system and its adaptive control," International Journal of PharmTech Research, vol. 8, no. 8, pp. 79-94, 2015.
- [56] S. Vaidyanathan, "Output regulation of the forced Van der Pol chaotic oscillator via adaptive control method," International Journal of PharmTech Research, vol. 8, no. 6, pp. 106-116, 2015.
- [57] S. Vaidyanathan, "Sliding controller design for the global chaos synchronization of forced Van der Pol chaotic oscillators," International Journal of PharmTech Research, vol. 8, no. 7, pp. 100-111, 2015.
- [58] S. Vaidyanathan, "Global chaos synchronization of the forced Van der Pol chaotic oscillators via adaptive control method," International Journal of PharmTech Research, vol. 8, no. 6, pp. 156-166, 2015.
- [59] S. Vaidyanathan, "Hybrid chaos synchronization of the FitzHugh-Nagumo chaotic neuron models via adaptive control method," International Journal of PharmTech Research, vol. 8, no. 8, pp. 48-60, 2015.
- [60] S. Vaidyanathan, "Global chaos synchronization of novel coupled Van der Pol conservative chaotic systems via adaptive control method," International Journal of PharmTech Research, vol. 8, no. 8, pp. 95-111, 2015.
- [61] S. Vaidyanathan, "3-cells Cellular Neural Network (CNN) attractor and its adaptive biological control," International Journal of PharmTech Research, vol. 8, no. 4, pp. 632-640, 2015.
- [62] S. Vaidyanathan, "Adaptive chaotic synchronization of enzymes substrates system with ferroelectric behaviour in brain waves," International Journal of PharmTech Research, vol. 8, no. 5, pp. 964-973, 2015.
- [63] S. Vaidyanathan, "Chaos in neurons and synchronization of Birkhoff-Shaw strange chaotic attractors via adaptive control," International Journal of PharmTech Research, vol. 8, no. 6, pp. 1-11, 2015.
- [64] S. Vaidyanathan, "Hybrid chaos synchronization of 3-cells cellular neural network attractors via adaptive control method," International Journal of PharmTech Research, vol. 8, no. 8, pp. 61-73, 2015.
- [65] S. Vaidyanathan, "Synchronization of 3-cells cellular neural network (CNN) attractors via adaptive control method," International Journal of PharmTech Research, vol. 8, no. 5, pp. 946-955, 2015.
- [66] S. Vaidyanathan, "Global chaos control of 3-cells cellular neural network attractor via integral sliding mode control," International Journal of PharmTech Research, vol. 8, no. 8, pp. 211-221, 2015.
- [67] S. Vaidyanathan, "Global chaos synchronization of 3-cells cellular neural network attractors via integral sliding mode control," International Journal of PharmTech Research, vol. 8, no. 8, pp. 118-130, 2015.
- [68] S. Vaidyanathan, "Anti-synchronization of 3-cells cellular neural network attractors via adaptive control method," International Journal of PharmTech Research, vol. 8, no. 7, pp. 26-38, 2015.
- [69] S. Vaidyanathan, "Sliding controller design for the global chaos synchronization of enzymes-substrates systems," International Journal of PharmTech Research, vol. 8, no. 7, pp. 89-99, 2015.
- [70] S. Vaidyanathan, "Chaos in neurons and adaptive control of Birkhoff-Shaw strange chaotic attractor," International Journal of PharmTech Research, vol. 8, no. 5, pp. 956-963, 2015.
- [71] S. Vaidyanathan, "Active control design for the anti-synchronization of Lotka-Volterra biological systems with four competitive species," International Journal of PharmTech Research, vol. 8, no. 7, pp. 58-70, 2015.
- [72] S. Vaidyanathan, "Global chaos synchronization of the Lotka-Volterra biological systems with four competitive species via active control," International Journal of PharmTech Research, vol. 8, no. 6, pp. 206-217, 2015.
- [73] S. Vaidyanathan, "Active control design for the hybrid chaos synchronization of Lotka-Volterra biological systems with four competitive species," International Journal of PharmTech Research, vol. 8, no. 8, pp. 30-42, 2015.
- [74] S. Vaidyanathan, "Adaptive biological control of generalized Lotka-Volterra three-species biological system," International Journal of PharmTech Research, vol. 8, no. 4, pp. 622-631, 2015.
- [75] S. Vaidyanathan, "Lotka-Volterra two species competitive biology models and their ecological monitoring," International Journal of PharmTech Research, vol. 8, no. 6, pp. 32-44, 2015.
- [76] S. Vaidyanathan, "Adaptive synchronization of generalized Lotka-Volterra three-species biological systems," International Journal of PharmTech Research, vol. 8, no. 5, pp. 928-937, 2015.
- [77] S. Vaidyanathan, "Anti-synchronization of the generalized Lotka-Volterra three-species biological systems via adaptive control," International Journal of PharmTech Research, vol. 8, no. 8, pp. 141-156, 2015.
- [78] V.-T. Pham, C.K. Volos, S. Vaidyanathan, T.P. Le and V.Y. Vu, "A memristor-based hyperchaotic system with hidden attractors: Dynamics, synchronization and circuitual emulating," Journal of Engineering Science and Technology Review, vol. 8, no. 2, pp. 205-214, 2015.
- [79] V.-T. Pham, C. Volos, S. Jafari, X. Wang and S. Vaidyanathan, "Hidden hyperchaotic attractor in a novel simple memristive neural network," Optoelectronics and Advanced Materials, Rapid Communications, vol. 8, nos. 11-12, pp. 1157-1163, 2014.
- [80] C.K. Volos, I.M. Kyprianidis, I.N. Stouboulos, E. Tlelo-Cuautle and S. Vaidyanathan, "Memristor: A new concept in synchronization of coupled neuromorphic circuits," Journal of Engineering Science and Technology Review, vol. 8, no. 2, pp. 157-173, 2015.
- [81] O.I. Tacha, Ch. K. Volos, I.N. Stouboulos, S. Vaidyanathan and V.-T. Pham, "Analysis, adaptive control and circuit simulation of a novel nonlinear finance system," Applied Mathematics and Computation, vol. 276, pp. 200-217, 2016.

- [82] H.W. Lorenz, *Nonlinear Dynamical Economics and Chaotic Motion*, Springer, Berlin, Germany, 1993.
- [83] V. Sundarapandian, "Output regulation of the Lorenz attractor," *Far East Journal of Mathematical Sciences*, vol. 42, no. 2, pp. 289-299, 2010.
- [84] S. Vaidyanathan and S. Rasappan, "New results on the global chaos synchronization for Liu-Chen-Liu and Lü chaotic systems," *Communications in Computer and Information Science*, vol. 102, pp. 20-27, 2010.
- [85] S. Vaidyanathan and K. Rajagopal, "Anti-synchronization of Li and T chaotic systems by active nonlinear control," *Communications in Computer and Information Science*, vol. 198, pp. 175-184, 2011.
- [86] S. Vaidyanathan and S. Rasappan, "Global chaos synchronization of hyperchaotic Bao and Xu systems by active nonlinear control," *Communications in Computer and Information Science*, vol. 198, pp. 10-17, 2011.
- [87] S. Vaidyanathan, "Output regulation of the unified chaotic system," *Communications in Computer and Information Science*, vol. 198, pp. 1-9, 2011.
- [88] S. Vaidyanathan and K. Rajagopal, "Global chaos synchronization of hyperchaotic Pang and Wang systems by active nonlinear control," *Communications in Computer and Information Science*, vol. 204, pp. 84-93, 2011.
- [89] S. Vaidyanathan, "Hybrid chaos synchronization of Liu and Lü systems by active nonlinear control," *Communications in Computer and Information Science*, vol. 204, pp. 1-10, 2011.
- [90] P. Sarasu and V. Sundarapandian, "Active controller design for generalized projective synchronization of four-scroll chaotic systems," *International Journal of Systems Signal Control and Engineering Application*, vol. 4, no. 2, pp. 26-33, 2011.
- [91] S. Vaidyanathan and S. Rasappan, "Hybrid synchronization of hyperchaotic Qi and Lü systems by nonlinear control," *Communications in Computer and Information Science*, vol. 131, pp. 585-593, 2011.
- [92] S. Vaidyanathan and K. Rajagopal, "Hybrid synchronization of hyperchaotic Wang-Chen and hyperchaotic Lorenz systems by active non-linear control," *International Journal of Systems Signal Control and Engineering Application*, vol. 4, no. 3, pp. 55-61, 2011.
- [93] S. Vaidyanathan, "Output regulation of Arneodo-Couillet chaotic system," *Communications in Computer and Information Science*, vol. 133, pp. 98-107, 2011.
- [94] P. Sarasu and V. Sundarapandian, "The generalized projective synchronization of hyperchaotic Lorenz and hyperchaotic Qi systems via active control," *International Journal of Soft Computing*, vol. 6, no. 5, pp. 216-223, 2011.
- [95] S. Vaidyanathan, "Output regulation of the Liu chaotic system," *Applied Mechanics and Materials*, vol. 110-116, pp. 3982-2989, 2012.
- [96] V. Sundarapandian and R. Karthikeyan, "Hybrid synchronization of hyperchaotic Lorenz and hyperchaotic Chen systems via active control," *Journal of Engineering Applied Sciences*, vol. 7, no. 3, pp. 254-264, 2012.
- [97] S. Vaidyanathan and S. Pakiriswamy, "Generalized projective synchronization of double-scroll chaotic systems using active feedback control," *Lecture Notes of the Institute for Computer Sciences, Social-Informatics and Telecommunications Engineering*, vol. 84, pp. 111-118, 2012.
- [98] S. Pakiriswamy and S. Vaidyanathan, "Generalized projective synchronization of three-scroll chaotic systems via active control," *Lecture Notes of the Institute for Computer Sciences, Social-Informatics and Telecommunications Engineering*, vol. 85, pp. 146-155, 2012.
- [99] S. Pakiriswamy and S. Vaidyanathan, "Generalized projective synchronization of hyperchaotic Lü and hyperchaotic Cai systems via active control," *Lecture Notes of the Institute for Computer Sciences, Social-Informatics and Telecommunications Engineering*, vol. 84, pp. 53-62, 2012.
- [100] R. Karthikeyan and V. Sundarapandian, "Hybrid chaos synchronization of four-scroll systems via active control," *Journal of Electrical Engineering*, vol. 65, no. 2, pp. 97-103, 2014.
- [101] S. Vaidyanathan and S. Pakiriswamy, "A 3-D novel conservative chaotic system and its generalized projective synchronization via adaptive control," *Journal of Engineering Science and Technology Review*, vol. 8, no. 2, pp. 52-60, 2015.
- [102] S. Vaidyanathan, "Global chaos synchronization of Mathieu-Van der Pol chaotic systems via adaptive control method," *International Journal of ChemTech Research*, vol. 8, no. 10, pp. 148-162, 2015.
- [103] S. Vaidyanathan, C.K. Volos and V.-T. Pham, "Analysis, control, synchronization and SPICE implementation of a novel 4-D hyperchaotic Rikitake dynamo system without equilibrium," *Journal of Engineering Science and Technology Review*, vol. 8, no. 2, pp. 232-244, 2015.
- [104] S. Vaidyanathan, V.-T. Pham and C.K. Volos, "A 5-D hyperchaotic Rikitake dynamo system with hidden attractors," *European Physical Journal: Special Topics*, vol. 224, no. 8, pp. 1575-1592, 2015.
- [105] S. Vaidyanathan and A.T. Azar, "Analysis and control of a 4-D novel hyperchaotic system," *Studies in Computational Intelligence*, vol. 581, pp. 3-17, 2015.
- [106] S. Vaidyanathan, "Anti-synchronization of Mathieu-Van der Pol chaotic systems via adaptive control method," *International Journal of ChemTech Research*, vol. 8, no. 11, pp. 638-653, 2015.
- [107] S. Vaidyanathan, "Hyperchaos, qualitative analysis, control and synchronisation of a ten-term 4-D hyperchaotic system with an exponential nonlinearity and three quadratic nonlinearities," *International Journal of Modelling, Identification and Control*, vol. 23, no. 4, pp. 380-392, 2015.
- [108] S. Vaidyanathan and S. Pakiriswamy, "Adaptive controller design for the generalized projective synchronization of circulant chaotic systems with

- unknown parameters,” *International Journal of Control Theory and Applications*, vol. 7, no. 1, pp. 55-74, 2014.
- [109] S. Vaidyanathan, “Qualitative analysis and control of an eleven-term novel 4-D hyperchaotic system with two quadratic nonlinearities,” *International Journal of Control Theory and Applications*, vol. 7, no. 1, pp. 35-47, 2014.
- [110] V.-T. Pham, C. Volos, S. Jafari, X. Wang and S. Vaidyanathan, “Hidden hyperchaotic attractor in a novel simple memristive neural network,” *Optoelectronics and Advanced Materials, Rapid Communications*, vol. 8, nos. 11-12, pp. 1157-1163, 2014.
- [111] S. Vaidyanathan, C. Volos and V.-T. Pham, “Hyperchaos, adaptive control and synchronization of a novel 5-D hyperchaotic system with three positive Lyapunov exponents and its SPICE implementation,” *Archives of Control Sciences*, vol. 24, no. 4, pp. 409-446, 2014.
- [112] V. Sundarapandian, “Adaptive control and synchronization design for the Lu-Xiao chaotic system,” *Lecture Notes in Electrical Engineering*, vol. 131, pp. 319-327, 2013.
- [113] S. Vaidyanathan, “Analysis, control and synchronization of hyperchaotic Zhou system via adaptive control,” *Advances in Intelligent Systems and Computing*, vol. 177, pp. 1-10, 2013.
- [114] S. Vaidyanathan and S. Pakiriswamy, “Generalized projective synchronization of six-term Sundarapandian chaotic systems by adaptive control,” *International Journal of Control Theory and Applications*, vol. 6, no. 2, pp. 153-163, 2013.
- [115] S. Vaidyanathan, “A ten-term novel 4-D hyperchaotic system with three quadratic nonlinearities and its control,” *International Journal of Control Theory and Applications*, vol. 6, no. 2, pp. 97-109, 2013.
- [116] S. Vaidyanathan, “Anti-synchronization of Sprott-L and Sprott-M chaotic systems via adaptive control,” *International Journal of Control Theory and Applications*, vol. 5, no. 1, pp. 41-59, 2012.
- [117] P. Sarasu and V. Sundarapandian, “Adaptive controller design for the generalized projective synchronization of 4-scroll systems,” *International Journal of Systems Signal Control and Engineering Application*, vol. 5, no. 2, pp. 21-30, 2012.
- [118] P. Sarasu and V. Sundarapandian, “Generalized projective synchronization of two-scroll systems via adaptive control,” *International Journal of Soft Computing*, vol. 7, no. 4, pp. 146-156, 2012.
- [119] S. Vaidyanathan and K. Rajagopal, “Global chaos synchronization of hyperchaotic Pang and hyperchaotic Wang systems via adaptive control,” *International Journal of Soft Computing*, vol. 7, no. 1, pp. 28-37, 2012.
- [120] V. Sundarapandian and R. Karthikeyan, “Anti-synchronization of Lü and Pan chaotic systems by adaptive nonlinear control,” *European Journal of Scientific Research*, vol. 64, no. 1, pp. 94-106, 2011.
- [121] S. Vaidyanathan, C.K. Volos, K. Rajagopal, I.M. Kyprianidis and I.N. Stouboulos, “Adaptive backstepping controller design for the anti-synchronization of identical WINDMI chaotic systems with unknown parameters and its SPICE implementation,” *Journal of Engineering Science and Technology Review*, vol. 8, no. 2, pp. 74-82, 2015.
- [122] S. Vaidyanathan, B.A. Idowu and A.T. Azar, “Backstepping controller design for the global chaos synchronization of Sprott’s jerk systems,” *Studies in Computational Intelligence*, vol. 581, pp. 39-58, 2015.
- [123] S. Vaidyanathan and S. Rasappan, “Global chaos synchronization of n-scroll Chua circuit and Lur’e system using backstepping control design with recursive feedback,” *Arabian Journal for Science and Engineering*, vol. 39, no. 4, pp. 3351-3364, 2014.
- [124] S. Rasappan and S. Vaidyanathan, “Global chaos synchronization of WINDMI and Couillet chaotic systems using adaptive backstepping control design,” *Kyungpook Mathematical Journal*, vol. 54, no. 1, pp. 293-320, 2014.
- [125] S. Rasappan and S. Vaidyanathan, “Hybrid synchronization of n-scroll chaotic Chua circuits using adaptive backstepping control design with recursive feedback,” *Malaysian Journal of Mathematical Sciences*, vol. 7, no. 2, pp. 219-246, 2013.
- [126] R. Suresh and V. Sundarapandian, “Global chaos synchronization of a family of n-scroll hyperchaotic Chua circuits using backstepping control with recursive feedback,” *Far East Journal of Mathematical Sciences*, vol. 73, no. 1, pp. 73-95, 2013.
- [127] S. Rasappan and S. Vaidyanathan, “Synchronization of hyperchaotic Liu system via backstepping control with recursive feedback,” *Communications in Computer and Information Science*, vol. 305, pp. 212-221, 2012.
- [128] S. Rasappan and S. Vaidyanathan, “Global chaos synchronization of WINDMI and Couillet chaotic systems by backstepping control,” *Far East Journal of Mathematical Sciences*, vol. 67, no. 2, pp. 265-287, 2012.
- [129] S. Vaidyanathan and S. Rasappan, “Global chaos synchronization of Chen-Lee systems via backstepping control,” *IEEE-International Conference on Advances in Engineering, Science and Management, ICAESM-2012*, art. No. 6216312, pp. 73-77, 2012.
- [130] S. Vaidyanathan, C. Volos, V.-T. Pham and K. Madhavan, “Analysis, adaptive control and synchronization of a novel 4-D hyperchaotic hyperjerk system and its SPICE implementation,” *Archives of Control Sciences*, vol. 25, no. 1, pp. 135-158, 2015.
- [131] S. Vaidyanathan, “Global chaos synchronization of Duffing double-well chaotic oscillators via integral sliding mode control,” *International Journal of ChemTech Research*, vol. 8, no. 11, pp. 141-151, 2015.
- [132] S. Vaidyanathan, S. Sampath and A.T. Azar, “Global chaos synchronisation of identical chaotic systems via novel sliding mode control method and its application to Zhu system,” *International Journal of Modelling, Identification and Control*, vol. 23, no. 1, pp. 92-100, 2015.

- [133] S. Vaidyanathan, "Global chaos synchronization of Rucklidge chaotic systems for double convection via sliding mode control," *International Journal of ChemTech Research*, vol. 8, no. 8, pp. 61-72, 2015.
- [134] S. Vaidyanathan and A.T. Azar, "Hybrid synchronization of identical chaotic systems using sliding mode control and an application to Vaidyanathan chaotic systems," *Studies in Computational Intelligence*, vol. 576, pp. 549-569, 2015.
- [135] S. Vaidyanathan and A.T. Azar, "Anti-synchronization of identical chaotic systems using sliding mode control and an application to Vaidyanathan-Madhavan chaotic systems," *Studies in Computational Intelligence*, vol. 576, pp. 527-547, 2015.
- [136] S. Vaidyanathan, "Global chaos synchronisation of identical Li-Wu chaotic systems via sliding mode control," *International Journal of Web and Grid Services*, vol. 22, no. 2, pp. 170-177, 2014.
- [137] S. Vaidyanathan, "Sliding mode control based global chaos control of Liu-Liu-Liu-Su chaotic system," *International Journal of Control Theory and Applications*, vol. 5, no. 1, pp. 15-20, 2012.
- [138] S. Vaidyanathan, "Global chaos control of hyperchaotic Liu system via sliding control method," *International Journal of Control Theory and Applications*, vol. 5, no. 2, pp. 117-123, 2012.
- [139] V. Sundarapandian and S. Sivaperumal, "Sliding controller design of hybrid synchronization of four-wing chaotic systems," *International Journal of Soft Computing*, vol. 6, no. 5, pp. 224-231, 2011.
- [140] S. Vaidyanathan and S. Sampath, "Anti-synchronization of four-wing chaotic systems via sliding mode control," *International Journal of Automation and Computing*, vol. 9, no. 3, pp. 274-279, 2012.
- [141] Y. Li and C. Li, "Complete synchronization of delayed chaotic neural networks by intermittent control with two switches in a control period," *Neurocomputing*, vol. 173, pp. 1341-1347, 2016.
- [142] S. Pourdehi, P. Karimaghaee and D. Karimipour, "Adaptive controller design for lag-synchronization of non-identical time-delayed chaotic systems with unknown parameters," *Physics Letters A*, vol. 375, no. 17, pp. 1769-1778, 2011.
- [143] Z. Wang and X. Shi, "Lag synchronization of two identical Hindmarsh-Rose systems with mismatched parameters and external disturbance via a single sliding mode controller," *Applied Mathematics and Computation*, vol. 218, no. 22, pp. 10914-10922, 2012.
- [144] L. Wang and W. Ding, "Synchronization for delayed non-autonomous reaction-diffusion fuzzy cellular neural networks," *Communications in Nonlinear Science and Numerical Simulation*, vol. 17, no. 1, pp. 170-182, 2012.
- [145] H.K. Khalil, *Nonlinear Systems*, Prentice Hall, New Jersey, 2001.